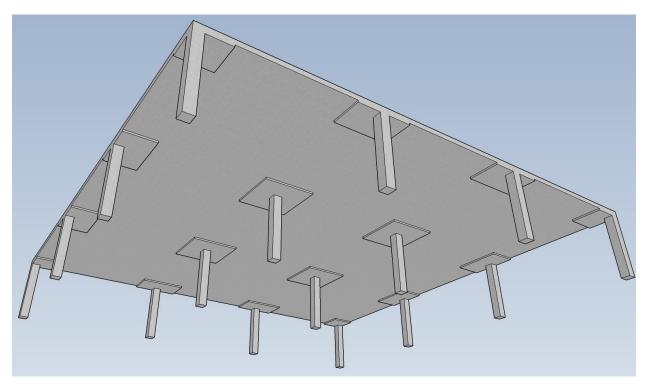
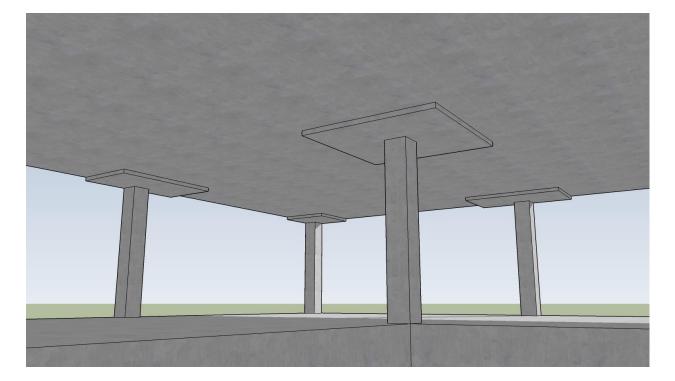




Two-Way Flat Slab (Concrete Floor with Drop Panels) System Analysis and Design



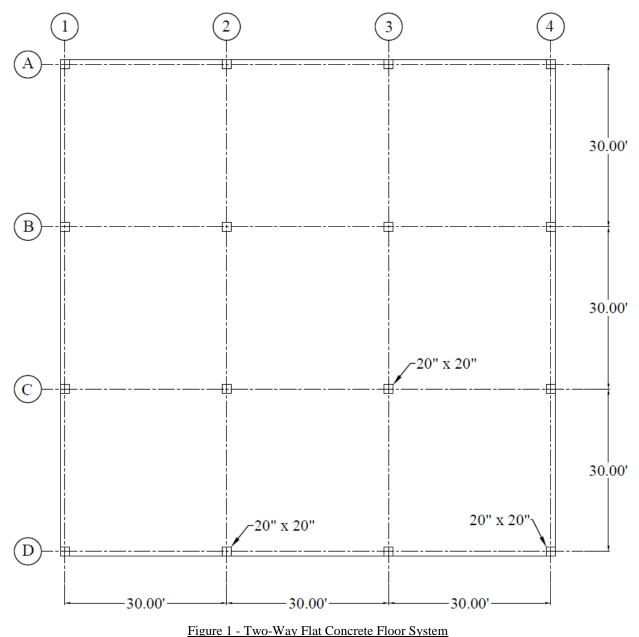






Two-Way Flat Slab (Concrete Floor with Drop Panels) System Analysis and Design

Design the concrete floor slab system shown below for an intermediate floor considering partition weight = 20 psf, and unfactored live load = 60 psf. The lateral loads are independently resisted by shear walls. The use of flat plate system will be checked. If the use of flat plate is not adequate, the use of flat slab system with drop panels will be investigated. Flat slab concrete floor system is similar to the flat plate system. The only exception is that the flat slab uses drop panels (thickened portions around the columns) to increase the nominal shear strength of the concrete at the critical section around the columns. The Equivalent Frame Method (EFM) shown in ACI 318 is used in this example. The hand solution from EFM is also used for a detailed comparison with the model results of spSlab engineering software program.





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ASCE/SEI 7-10 (Table C3-1)

ASCE/SEI 7-10 (Table 4-1)

ACI 318-14 (8.3.1.1)

ACI 318-14 (8.3.1.1(a))

ACI 318-14 (8.3.1.1(a))

ACI 318-14 (Table 8.3.1.1)

Structure Point

Code

Building Code Requirements for Structural Concrete (ACI 318-14) and Commentary (ACI 318R-14)

Reference

Concrete Floor Systems (Guide to Estimating and Economizing), Second Edition, 2002 David A. Fanella

Notes on ACI 318-11 Building Code Requirements for Structural Concrete, Twelfth Edition, 2013 Portland Cement Association.

Simplified Design of Reinforced Concrete Buildings, Fourth Edition, 2011 Mahmoud E. Kamara and Lawrence C. Novak

Control of Deflection in Concrete Structures (ACI 435R-95)

Design Data

Story Height = 13 ft (provided by architectural drawings)

Superimposed Dead Load, SDL = 20 psf for framed partitions, wood studs, 2 x 2, plastered 2 sides

Live Load, LL = 60 psf

50 psf is considered by inspection of Table 4-1 for Office Buildings – Offices (2/3 of the floor area)

80 psf is considered by inspection of Table 4-1 for Office Buildings - Corridors (1/3 of the floor area)

 $LL = 2/3 \times 50 + 1/3 \times 80 = 60 \text{ psf}$

 f_c ' = 5000 psi (for slab)

 f_c ' = 6000 psi (for columns)

 $f_y = 60,000 \text{ psi}$

Solution

1. Preliminary member sizing

For Flat Plate (without Drop Panels)

a. <u>Slab minimum thickness – Deflection</u>

In lieu of detailed calculation for deflections, ACI 318 Code gives minimum slab thickness for two-way construction without interior beams in *Table 8.3.1.1*.

For this flat plate slab systems the minimum slab thicknesses per ACI 318-14 are:

Exterior Panels: $h_s = \frac{l_n}{30} = \frac{340}{30} = 11.33$ in.	ACI 318-14 (Table 8.3.1.1)
--	----------------------------

But not less than 5 in.

Interior Panels:
$$h_s = \frac{l_n}{33} = \frac{340}{33} = 10.3$$
 in.

But not less than 5 in.

Where $l_n =$ length of clear span in the long direction = $30 \times 12 - 20 = 340$ in.



Try 11 in. slab for all panels (self-weight = 150 pcf x 11 in / 12 = 137.5 psf)

b. <u>Slab shear strength – one way shear</u>

Evaluate the average effective depth (Figure 2):

$$d_{l} = h_{s} - c_{clear} - d_{b} - \frac{d_{b}}{2} = 11 - 0.75 - 0.75 - \frac{0.75}{2} = 9.13 \text{ in.}$$
$$d_{t} = h_{s} - c_{clear} - \frac{d_{b}}{2} = 11 - 0.75 - \frac{0.75}{2} = 9.88 \text{ in.}$$
$$d_{avg} = \frac{d_{l} + d_{t}}{2} = \frac{9.13 + 9.88}{2} = 9.51 \text{ in.}$$

Where:

$$c_{clear} = 3/4$$
 in. for # 6 steel bar

$$d_b = 0.75$$
 in. for # 6 steel bar

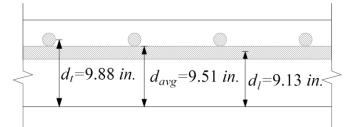


Figure 2 - Two-Way Flat Concrete Floor System

Factored dead load, $q_{Du} = 1.2 \times (137.5 + 20) = 189 \text{ psf}$

Factored live load, $q_{Lu} = 1.6 \times 60 = 96 \text{ psf}$

Total factored load, $q_u = 189 + 96 = 285 \text{ psf}$

Check the adequacy of slab thickness for beam action (one-way shear)

ACI 318-14 (22.5)

ACI 318-14 (5.3.1)

ACI 318-14 (Table 20.6.1.3.1)

at an interior column:

Consider a 12-in. wide strip. The critical section for one-way shear is located at a distance *d*, from the face of support (see Figure 3):

Tributary are for one-way shear is
$$A_{Tributary} = \left[\frac{30}{2} - \frac{20}{2 \times 12} - \frac{9.51}{12}\right] \times \frac{12}{12} = 13.37 \text{ ft}^2$$

 $V_u = q_u \times A_{Tributary} = 0.285 \times 13.37 = 3.81 \text{ kips}$
 $V_c = 2\lambda \sqrt{f_c} b_w d$
ACI 318-14 (Eq. 22.5.5.1)



ACI 318-14 (Table 22.6.5.2(a))

Where $\lambda = 1$ for normal weight concrete

$$\varphi V_c = 0.75 \times 2 \times 1.0 \times \sqrt{5000} \times 12 \times \frac{9.51}{1000} = 12.09 \text{ kips} > V_u$$

Slab thickness of 11 in. is adequate for one-way shear.

c. <u>Slab shear strength - two-way shear</u>

Check the adequacy of slab thickness for punching shear (two-way shear) at an interior column (Figure 4):

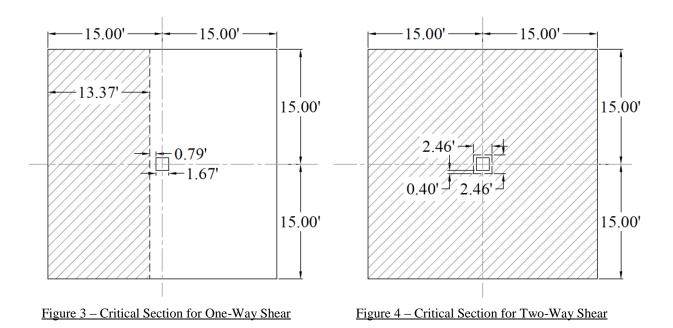
Tributary area for two-way shear is $A_{Tributary} = (30 \times 30) - \left(\frac{20 + 9.51}{12}\right)^2 = 894 \text{ ft}^2$

$$V_u = q_u \times A_{Tributary} = 0.285 \times 894 = 254.78$$
 kips

$$V_c = 4\lambda \sqrt{f_c} b_w d$$
 (For square interior column)

$$V_c = 4 \times \sqrt{5000} \times (4 \times (20 + 9.51)) \times \frac{9.51}{1000} = 317$$
 kips
 $\varphi V_c = 0.75 \times 317 = 237.8$ kips $< V_u$

Slab thickness of 11 in. is not adequate for two-way shear.



In this case, three options could be used: 1) to increase the slab thickness, 2) to use headed shear reinforcement, or 3) to use drop panels. In this example, the latter option will be used to achieve better understanding for the design of two-way slab with drop panels often called flat slab.

Check the drop panel dimensional limitations as follows:



1) The drop panel shall project below the slab at least one-fourth of the adjacent slab thickness.

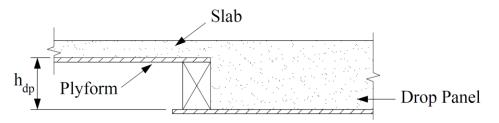
ACI 318-14 (8.2.4(a))

Since the slab thickness (h_s) is 10 in. (see page 6), the thickness of the drop panel should be at least: $h_{dp,min} = 0.25 \times h_s = 0.25 \times 10 = 2.5$ in.

Drop panel dimensions are also controlled by formwork considerations. The following Figure shows the standard lumber dimensions that are used when forming drop panels. Using other depths will unnecessarily increase formwork costs.

For nominal lumber size (2x), $h_{dp} = 4.25$ in. $> h_{dp, min} = 2.5$ in.

The total thickness including the slab and the drop panel (h) = $h_s + h_{dp} = 10 + 4.25 = 14.25$ in.



Nominal Lumber Size, in.	Actual Lumber Size, in.	Plyform Thickness, in.	h _{dp} , in.
2x	1 1/2	3/4	2 1/4
4x	3 1/2	3/4	4 1/4
6x	5 1/2	3/4	6 1/4
8x	7 1/4	3/4	8

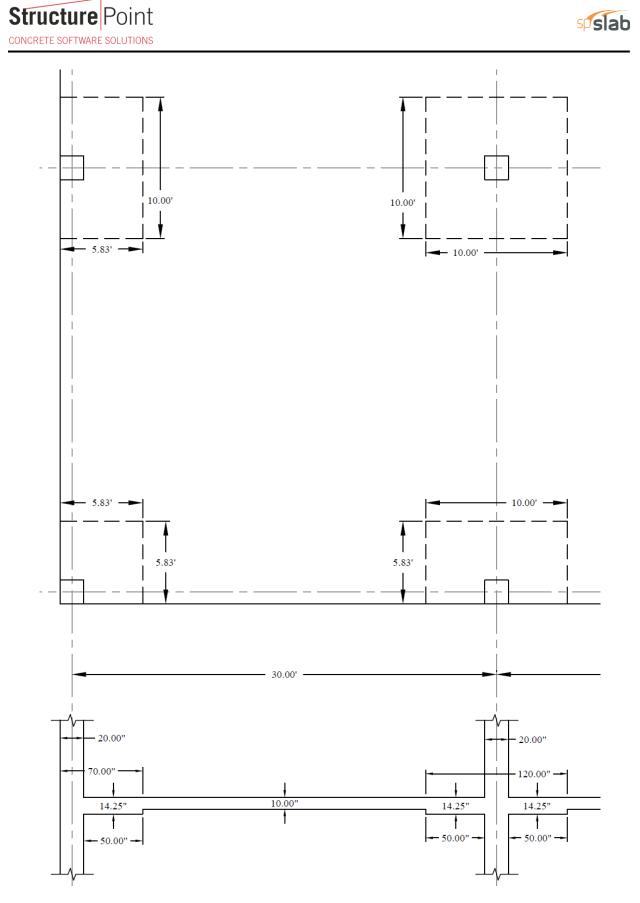
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2) The drop panel shall extend in each direction from the centerline of support a distance not less than onesixth the span length measured from center-to-center of supports in that direction.

ACI 318-14 (8.2.4(b))

$$L_{1,dp} = \frac{1}{6} \times L_1 + \frac{1}{6} \times L_1 = \frac{1}{6} \times 30 + \frac{1}{6} \times 30 = 5 \text{ ft}$$
$$L_{2,dp} = \frac{1}{6} \times L_2 + \frac{1}{6} \times L_2 = \frac{1}{6} \times 30 + \frac{1}{6} \times 30 = 5 \text{ ft}$$

Based on the previous discussion, Figure 6 shows the dimensions of the selected drop panels around interior, edge (exterior), and corner columns.







ACI 318-14 (8.3.1.1)

ACI 318-14 (8.3.1.1(b))

<u>ACI 318-14 (8.3.1.1(b))</u>

ACI 318-14 (Table 8.3.1.1)

For Flat Slab (with Drop Panels)

For slabs with changes in thickness and subjected to bending in two directions, it is necessary to check shear at multiple sections as defined in the *ACI 319-14*. The critical sections shall be located with respect to:

1) Edges or corners of columns.	<u>ACI 318-14 (22.6.4.1(a))</u>
2) Changes in slab thickness, such as edges of drop panels.	<u>ACI 318-14 (22.6.4.1(b))</u>

a. <u>Slab minimum thickness – Deflection</u>

In lieu of detailed calculation for deflections, ACI 318 Code gives minimum slab thickness for two-way construction without interior beams in *Table 8.3.1.1*.

For this flat plate slab systems the minimum slab thicknesses per ACI 318-14 are:

Exterior Panels: $h_s = \frac{l_n}{33} = \frac{340}{33} = 10.30$ in.	<u>ACI 318-14 (Table 8.3.1.1)</u>
--	-----------------------------------

But not less than 4 in.

Interior Panels:
$$h_s = \frac{l_n}{36} = \frac{340}{36} = 9.44$$
 in.

But not less than 4 in.

Where l_n = length of clear span in the long direction = 30 x 12 - 20 = 340 in.

Try 10 in. slab for all panels

Self-weight for slab section without drop panel = $150 \text{ pcf } x \ 10 \text{ in}$. /12 = 125 psfSelf-weight for slab section with drop panel = $150 \text{ pcf } x \ 14.25 \text{ in}$. /12 = 178 psf

b. <u>Slab shear strength – one way shear</u>

For critical section at distance *d* from the edge of the column (slab section with drop panel): Evaluate the average effective depth:

$$d_{l} = h_{s} - c_{clear} - d_{b} - \frac{d_{b}}{2} = 14.25 - 0.75 - 0.75 - \frac{0.75}{2} = 12.38 \text{ in}$$
$$d_{t} = h_{s} - c_{clear} - \frac{d_{b}}{2} = 14.25 - 0.75 - \frac{0.75}{2} = 13.13 \text{ in.}$$
$$d_{avg} = \frac{d_{l} + d_{r}}{2} = \frac{12.38 + 13.13}{2} = 12.75 \text{ in.}$$

Where:

 $c_{clear} = 3/4$ in. for # 6 steel bar

 $d_b = 0.75$ in. for # 6 steel bar

ACI 318-14 (Table 20.6.1.3.1)



Factored dead load $\rightarrow q_{Du} = 1.2 \times (178 + 20) = 237.6 \text{ psf}$

Factored live load $\rightarrow q_{Lu} = 1.6 \times 60 = 96 \text{ psf}$

Total factored load $\rightarrow q_u = 237.6 + 96 = 333.6 \text{ psf}$

Check the adequacy of slab thickness for beam action (one-way shear) from the edge of the interior column

ACI 318-14 (22.5)

ACI 318-14 (5.3.1)

Consider a 12-in. wide strip. The critical section for one-way shear is located at a distance d, from the edge of the column (see Figure 7)

Tributary area for one-way shear is $A_{Tributary} = \left[\frac{30}{2} - \frac{20}{2 \times 12} - \frac{12.75}{12}\right] \times \frac{12}{12} = 13.10 \text{ ft}^2$

$$V_u = q_u \times A_{Tributary} = 0.334 \times 13.10 = 4.37$$
 kips

$$V_c = 2\lambda \sqrt{f_c} b_w d$$
 ACI 318-14 (Eq. 22.5.5.1)

Where $\lambda = 1$ for normal weight concrete

$$\varphi V_c = 0.75 \times 2 \times 1.0 \times \sqrt{5000} \times 12 \times \frac{12.75}{1000} = 16.23 \text{ kips} > V_u$$

Slab thickness of 14.25 in. is adequate for one-way shear for the first critical section (from the edge of the column).

For critical section at distance *d* from the edge of the drop panel (slab section without drop panel): Evaluate the average effective depth:

$$d_l = h_s - c_{clear} - d_b - \frac{d_b}{2} = 10 - 0.75 - 0.75 - \frac{0.75}{2} = 8.13$$
 in.

$$d_t = h_s - c_{clear} - \frac{d_b}{2} = 10 - 0.75 - \frac{0.75}{2} = 8.88$$
 in.

Total factored load $\rightarrow q_u = 174 + 96 = 270 \text{ psf}$

$$d_{avg} = \frac{d_l + d_r}{2} = \frac{8.13 + 8.88}{2} = 8.51$$
 in.

Where:

$$c_{clear} = 3/4$$
 in. for # 6 steel bar

 $d_b = 0.75$ in. for # 6 steel bar

Factored dead load $\rightarrow q_{Du} = 1.2 \times (125 + 20) = 174 \text{ psf}$ Factored live load $\rightarrow q_{Lu} = 1.6 \times 60 = 96 \text{ psf}$ ACI 318-14 (5.3.1)

7

ACI 318-14 (Table 20.6.1.3.1)



Check the adequacy of slab thickness for beam action (one-way shear) from the edge of the interior drop panel <u>ACI 318-14 (22.5)</u>

Consider a 12-in. wide strip. The critical section for one-way shear is located at a distance d, from the face of support (see Figure 7)

Tributary area for one-way shear is
$$A_{Tributary} = \left[\frac{30}{2} - \frac{20}{2} - \frac{8.51}{12}\right] \times \frac{12}{12} = 13.46 \text{ ft}^2$$

$$V_u = q_u \times A_{Tributary} = 0.270 \times 13.46 = 3.63$$
 kips

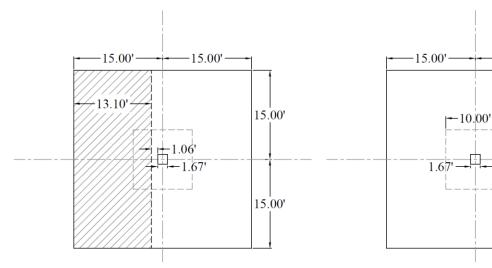
$$V_c = 2\lambda \sqrt{f_c'} b_w d$$

ACI 318-14 (Eq. 22.5.5.1)

Where $\lambda = 1$ for normal weight concrete

$$\varphi V_c = 0.75 \times 2 \times 1.0 \times \sqrt{5000} \times 12 \times \frac{8.51}{1000} = 10.82 \text{ kips} > V_u$$

Slab thickness of 10 in. is adequate for one-way shear for the second critical section (from the edge of the drop panel).



Critical Section from the Edge of the Column

Critical Section from the edge of the Drop Panel

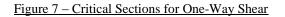
15.00'

9.29'

≁0.71'

15.00'

15.00'



c. <u>Slab shear strength – two-way shear</u>

For critical section at distance *d*/2 from the edge of the column (slab section with drop panel):

Check the adequacy of slab thickness for punching shear (two-way shear) at an interior column (Figure 8):

Tributary area for two-way shear is
$$A_{Tributary} = (30 \times 30) - \left(\frac{20 + 12.75}{12}\right)^2 = 892.6 \text{ ft}^2$$

$$V_u = q_u \times A_{Tributary} = 0.334 \times 892.6 = 297.9$$
 kips



ACI 318-14 (Table 22.6.5.2(a))

 $V_c = 4\lambda \sqrt{f_c} b_o d$ (For square interior column)

$$V_c = 4 \times \sqrt{5000} \times (4 \times (20 + 12.75)) \times \frac{12.75}{1000} = 472 \text{ kips}$$

$$\varphi V_c = 0.75 \times 472 = 354 \text{ kips} > V_u$$

Slab thickness of 14.25 in. is adequate for two-way shear for the first critical section (from the edge of the column).

For critical section at distance d/2 from the edge of the drop panel (slab section without drop panel):

Check the adequacy of slab thickness for punching shear (two-way shear) at an interior drop panel (Figure 8):

Tributary area for two-way shear is $A_{Tributary} = (30 \times 30) - \left(\frac{120 + 8.51}{12}\right)^2 = 785 \text{ ft}^2$

 $V_u = q_u \times A_{Tributary} = 0.270 \times 785 = 212.04$ kips

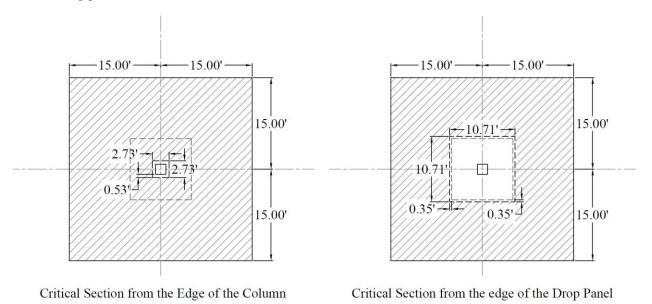
 $V_c = 4\lambda \sqrt{f_c} b_o d$ (For square interior column)

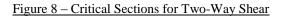
ACI 318-14 (Table 22.6.5.2(a))

$$V_c = 4 \times \sqrt{5000} \times (4 \times (120 + 8.51)) \times \frac{8.51}{1000} = 1236 \text{ kips}$$

 $\varphi V_c = 0.75 \times 1236 = 927 \text{ kips} > V_u$

Slab thickness of 10 in. is adequate for two-way shear for the second critical section (from the edge of the drop panel).







d. Column dimensions - axial load

Check the adequacy of column dimensions for axial load:

Tributary area for interior column for live load, superimposed dead load, and self-weight of the slab is

 $A_{Tributary} = 30 \times 30 = 900 \text{ft}^2$

Tributary area for interior column for self-weight of additional slab thickness due to the presence of the drop panel is

 $A_{Tributary} = 10 \times 10 = 100 \text{ ft}^2$

Assuming five story building

 $P_u = n \times q_u \times A_{Tributary} = 5 \times (0.270 \times 900 + 0.0638 \times 100) = 1247$ kips

Assume 20 in. square column with 4 – No. 14 vertical bars with design axial strength, $\varphi P_{n,max}$ of

$$\varphi P_{n,\max} = 0.80 \varphi (0.85f'_c (A_g - A_{st}) + f_y A_{st})$$
ACI 318-14 (22.4.2)

$$\varphi P_{n,\text{max}} = 0.80 \times 0.65 \times (0.85 \times 6000 \times (20 \times 20 - 4 \times 2.25) + 60000 \times 4 \times 2.25) = 1,317,730 \text{ kips}$$

 $\varphi P_{n,\text{max}} = 1,318 \text{ kips} > P_u = 1,247 \text{ kips}$

Column dimensions of 20 in. x 20 in. are adequate for axial load.

2. Flexural Analysis and Design

ACI 318 states that a slab system shall be designed by any procedure satisfying equilibrium and geometric compatibility, provided that strength and serviceability criteria are satisfied. Distinction of two-systems from one-way systems is given by <u>ACI 318-14 (R8.10.2.3 & R8.3.1.2)</u>.

ACI 318 permits the use of Direct Design Method (DDM) and Equivalent Frame Method (EFM) for the gravity load analysis of orthogonal frames and is applicable to flat plates, flat slabs, and slabs with beams. The following sections outline the solution per EFM and spSlab software. For the solution per DDM, check the flat plate example.

2.1. Equivalent Frame Method (EFM)

EFM is the most comprehensive and detailed procedure provided by the ACI 318 for the analysis and design of two-way slab systems where the structure is modeled by a series of equivalent frames (interior and exterior) on column lines taken longitudinally and transversely through the building.

The equivalent frame consists of three parts (for a detailed discussion of this method, refer to <u>the flat plate</u> <u>design example</u>):

- 1) Horizontal slab-beam strip.
- 2) Columns or other vertical supporting members.



3) Elements of the structure (Torsional members) that provide moment transfer between the horizontal and vertical members.

2.1.1. Limitations for use of equivalent frame method

In EFM, live load shall be arranged in accordance with 6.4.3 which requires slab systems to be analyzed and designed for the most demanding set of forces established by investigating the effects of live load placed in various critical patterns. <u>ACI 318-14 (8.11.1.2 & 6.4.3)</u> Complete analysis must include representative interior and exterior equivalent frames in both the longitudinal and transverse directions of the floor. <u>ACI 318-14 (8.11.2.1)</u> Panels shall be rectangular, with a ratio of longer to shorter panel dimensions, measured center-to-center of supports, not to exceed 2. <u>ACI 318-14 (8.10.2.3)</u>

2.1.2. Frame members of equivalent frame

Determine moment distribution factors and fixed-end moments for the equivalent frame members. The moment distribution procedure will be used to analyze the equivalent frame. Stiffness factors k, carry over factors COF, and fixed-end moment factors FEM for the slab-beams and column members are determined using the design aids tables at <u>Appendix 20A of PCA Notes on ACI 318-11</u>. These calculations are shown below.

a. Flexural stiffness of slab-beams at both ends, K_{sb} .

$$\frac{c_{N1}}{\ell_1} = \frac{20}{(30 \times 12)} = 0.056 , \ \frac{c_{N2}}{\ell_2} = \frac{20}{(30 \times 12)} = 0.056$$
For $c_{F1} = c_{N1}$, stiffness factors, $k_{NF} = k_{FN} = 5.59$
Thus, $K_{sb} = k_{NF} \frac{E_{cs}I_s}{\ell_1} = 5.59 \frac{E_{cs}I_s}{\ell_1}$
 $PCA Notes on ACI 318-11 (Table A1)$
 $K_{sb} = 5.59 \times 4287 \times 10^3 \times \frac{30,000}{360} = 1,997 \times 10^6$ in.-lb
Where, $I_s = \frac{\ell_s h^3}{12} = \frac{360 \times (10)^3}{12} = 30,000$ in.⁴
 $E_{cs} = w_c^{1.5} 33\sqrt{f_c^2} = 150^{1.5} \times 33 \times \sqrt{5000} = 4287 \times 10^3$ psi
Carry-over factor $COF = 0.578$
Fixed-end moment, $FEM = \sum_{i=1}^{n} m_{NFi} \times w_i \times l_i^2$
Uniform load fixed end moment coefficient, $m_{NFI} = 0.0915$

Fixed end moment coefficient for (b-a) = 0.2 when a = 0, m_{NF2} = 0.0163 Fixed end moment coefficient for (b-a) = 0.2 when a = 0.8, m_{NF3} = 0.0163



b. Flexural stiffness of column members at both ends, K_c .

Referring to <u>Table A7, Appendix 20A</u>, <u>For the Bottom Column:</u> $t_a = 10/2 + 4.25 = 9.25 \text{ in}$, $t_b = 10/2 = 5 \text{ in}$. $\frac{t_a}{t_b} = \frac{9.25}{5} = 1.85$ H = 13 ft = 156 in, $H_c = 156 - 9.25 - 5 = 11.81 \text{ in}$. $\frac{H}{H_c} = \frac{156}{11.81} = 1.101$ Thus, $k_{AB} = 5.32$ and $C_{AB} = 0.54$ by interpolation. $K_{c,bottom} = \frac{5.32E_{cc}I_c}{\ell_c}$ $K_{c,bottom} = 5.32 \times 4696 \times 10^3 \times \frac{13,333}{156} = 2135.2 \times 10^6 \text{ in.-lb}$ Where $I_c = \frac{c^4}{12} = \frac{(20)^4}{12} = 13,333 \text{ in.}^4$ $E_{cc} = w_c^{15} 33\sqrt{f_c^2} = 150^{15} \times 33 \times \sqrt{6000} = 4696 \times 10^3 \text{ psi}$ $I_c = 13 \text{ ft} = 156 \text{ in.}$

For the Top Column:

$$\frac{t_b}{t_a} = \frac{5}{9.25} = 0.54$$
$$\frac{H}{H_c} = \frac{156}{11.81} = 1.101$$

Thus, $k_{BA} = 4.88$ and $C_{BA} = 0.59$ by interpolation.

$$K_{c} = \frac{4.88E_{cc}I_{c}}{\ell_{c}}$$
PCA Notes on ACI 318-11 (Table A7)
12.222

$$K_{c,top} = 4.88 \times 4696 \times 10^3 \times \frac{13,333}{156} = 1958.6 \times 10^6 \text{ in.-lb}$$

c. Torsional stiffness of torsional members, K_t .

$$K_{t} = \frac{9E_{cs}C}{\left[\ell_{2}\left(1 - \frac{c_{2}}{\ell_{2}}\right)^{3}\right]}$$
 ACI 318-14 (R.8.11.5)



ACI 318-14 (Eq. 8.10.5.2b)

$$K_{t} = \frac{9 \times 4287 \times 10^{3} \times 10632}{30 \times 12 \times (1 - 20/(30 \times 12))^{3}} = 1353 \times 10^{6} \text{ in.-lb}$$
Where $C = \sum (1 - 0.63 \frac{x}{y})(\frac{x^{3}y}{3})$

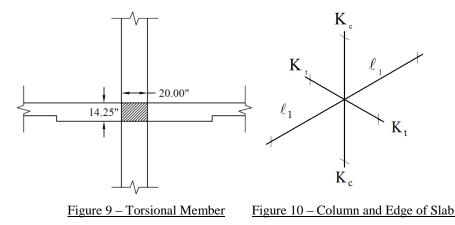
$$C = (1 - 0.63 \times \frac{14.25}{20})(14.25^{3} \times \frac{20}{3}) = 10632 \text{ in.}^{4}$$
 $c_{2} = 20 \text{ in.}, \ell_{2} = 30 \text{ ft} = 360 \text{ in.}$
Equivalent column stiffness K_{ec} .
$$K_{ec} = \frac{\sum K_{c} \times \sum K_{t}}{\sum K_{c} + \sum K_{t}}$$

$$K_{ec} = \frac{(2135.2 + 1958.6)(2 \times 1353)}{\sum K_{ec}} \times 10^{6}$$

$$K_{ec} = \frac{(2135.2 \pm 1958.) + (2 \times 1353)}{[(2135.2 \pm 1958.) + (2 \times 1353)]} \times$$

$$K_{ec} = 1353 \times 10^6$$
 in.-lb

Where $\sum K_t$ is for two torsional members one on each side of the column, and $\sum K_c$ is for the upper and lower columns at the slab-beam joint of an intermediate floor.



d. Slab-beam joint distribution factors, DF.

At exterior joint,

$$DF = \frac{1996}{(1996 + 1629)} = 0.551$$

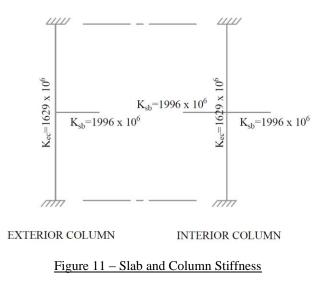
At interior joint,

$$DF = \frac{1996}{(1996 + 1996 + 1629)} = 0.355$$

COF for slab-beam =0.578







2.1.3. Equivalent frame analysis

Determine negative and positive moments for the slab-beams using the moment distribution method. Since the unfactored live load does not exceed three-quarters of the unfactored dead load, design moments are assumed to occur at all critical sections with full factored live on all spans. <u>ACI 318-14 (6.4.3.2)</u>

$$\frac{L}{D} = \frac{60}{(125 + 20)} = 0.41 < \frac{3}{4}$$

a. Factored load and Fixed-End Moments (FEM's).

For slab:

Factored dead load $q_{Du} = 1.2(125 + 20) = 174 \text{ psf}$

Factored live load $q_{Lu} = 1.6(60) = 96 \text{ psf}$

Factored load $q_u = q_{Du} + q_{Lu} = 270 \text{ psf}$

For drop panels:

Factored dead load $q_{Du} = 1.2(150 \times 4.25/12) = 63.75 \text{ psf}$

Factored live load $q_{Lu} = 1.6(0) = 0$ psf

Factored load $q_u = q_{Du} + q_{Lu} = 63.75 \text{ psf}$

Fixed-end moment, $FEM = \sum_{i=1}^{n} m_{NFi} \times w_i \times l_1^2$

 $FEM = 0.0915 \times 0.270 \times 30 \times 30^{2} + 0.0163 \times 0.0.064 \times 30/3 \times 30^{2} + 0.0163 \times 0.0.064 \times 30/3 \times 30^{2}$

FEM = 677.6 ft-kips

b. Moment distribution. Computations are shown in Table 1. Counterclockwise rotational moments acting on the member ends are taken as positive. Positive span moments are determined from the following equation:

PCA Notes on ACI 318-11 (Table A1)



$$M_{u,midspan} = M_o - \frac{(M_{uL} + M_{uR})}{2}$$

Where M_o is the moment at the midspan for a simple beam.

When the end moments are not equal, the maximum moment in the span does not occur at the midspan, but its value is close to that midspan for this example.

Positive moment in span 1-2:

$$M_{u} = (0.270 \times 30) \frac{30^{2}}{8} + 2 \times \left[\frac{(0.064 \times 30/6) \times 30/6}{2 \times 30} \times 30/6 \times (30 - 30/2) \right] - \frac{(331.7 + 807.6)}{2}$$

 $M_u = 349.6 \, \text{ft-kips}$

Table 1 - Moment Distribution for Equivalent Frame							
(+ 1		2	3	<i>m</i>	4		
Joint	1	2		3	5	4	
Member							
DF	0.551	0.355	0.355	0.355	0.355	0.551	
COF	0.578	0.578	0.578	0.578	0.578	0.578	
FEM	677.6	-677.6	677.6	-677.6	677.6	-677.6	
Dist	-373.1	0.0	0.0	0.0	0.0	373.1	
СО	0.0	-215.7	0.0	0.0	215.7	0.0	
Dist	0.0	76.6	76.6	-76.6	-76.6	0.0	
СО	44.3	0.0	-44.3	44.3	0.0	-44.3	
Dist	-24.4	15.7	15.7	-15.7	-15.7	24.4	
СО	9.1	-14.1	-9.1	9.1	14.1	-9.1	
Dist	-5.0	8.2	8.2	-8.2	-8.2	5.0	
СО	4.8	-2.9	-4.8	4.8	2.9	-4.8	
Dist	-2.6	2.7	2.7	-2.7	-2.7	2.6	
CO	1.6	-1.5	-1.6	1.6	1.5	-1.6	
Dist	-0.9	1.1	1.1	-1.1	-1.1	0.9	
CO	0.6	-0.5	-0.6	0.6	0.5	-0.6	
Dist	-0.4	0.4	0.4	-0.4	-0.4	0.4	
CO	0.2	-0.2	-0.2	0.2	0.2	-0.2	
Dist	-0.1	0.2	0.2	-0.2	-0.2	0.1	
CO	0.1	-0.1	-0.1	0.1	0.1	-0.1	
Dist	-0.1	0.1	0.1	-0.1	-0.1	0.1	
CO	0.0	0.0	0.0	0.0	0.0	0.0	
Dist	0.0	0.0	0.0	0.0	0.0	0.0	
M, k-ft	331.7	-807.6	721.9	-721.9	807.6	-331.7	
Midspan M, ft-kips	349.6		197.4		349.6		



2.1.4. Factored moments used for Design

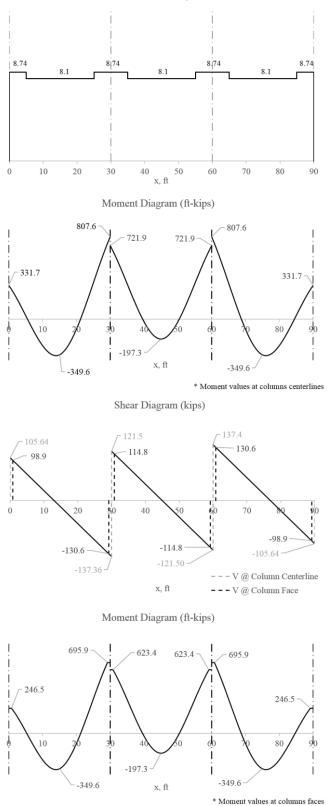
Positive and negative factored moments for the slab system in the direction of analysis are plotted in Figure 12. The negative moments used for design are taken at the faces of supports (rectangle section or equivalent rectangle for circular or polygon sections) but not at distances greater than 0.175 l_1 from the centers of supports. <u>ACI 318-14 (8.11.6.1)</u>

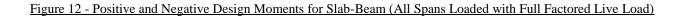
 $\frac{20 \text{ in.}}{12 \times 2} = 0.83 \text{ ft} < 0.175 \times 30 = 5.25 \text{ ft} \text{ (use face of supporting location)}$













2.1.5. Factored moments in slab-beam strip

a. Check whether the moments calculated above can take advantage of the reduction permitted by <u>ACI 318-</u> <u>14 (8.11.6.5)</u>:

If the slab system analyzed using EFM within the limitations of <u>ACI 318-14 (8.10.2)</u>, it is permitted by the ACI code to reduce the calculated moments obtained from EFM in such proportion that the absolute sum of the positive and average negative design moments need not exceed the total static moment M_o given by <u>Equation 8.10.3.2</u> in the <u>ACI 318-14</u>.

Check Applicability of Direct Design Method:

1. There is a minimum of three continuous spans in each direction.	<u>ACI 318-14 (8.10.2.1)</u>
2. Successive span lengths are equal.	<u>ACI 318-14 (8.10.2.2)</u>
3. Long-to-Short ratio is $30/30 = 1.0 < 2.0$.	<u>ACI 318-14 (8.10.2.3)</u>
4. Column are not offset.	<u>ACI 318-14 (8.10.2.4)</u>

- 5. Loads are gravity and uniformly distributed with service live-to-dead ratio of 0.41 < 2.0 (Note: The self-weight of the drop panels is not uniformly distributed entirely along the span. However, the variation in load magnitude is small).
- ACI 318-14 (8.10.2.5 and 6)

 6. Check relative stiffness for slab panel.
 ACI 318-14 (8.10.2.7)

Slab system is without beams and this requirement is not applicable.

All limitation of <u>ACI 318-14 (8.10.2)</u> are satisfied and the provisions of <u>ACI 318-14 (8.11.6.5)</u> may be applied:

$$M_o = \frac{q_u \ell_2 \ell_n^2}{8} = 0.270 \times 30 \times \frac{(30 - 20/12)^2}{8} = 812.8 \text{ ft-kips}$$

ACI 318-14 (Eq. 8.10.3.2)

End spans: $349.6 + \frac{331.7 + 807.6}{2} = 919.3$ ft-kips

Interior span:
$$197.3 + \frac{721.9 + 721.9}{2} = 919.2$$
ft-kips

To illustrate proper procedure, the interior span factored moments may be reduced as follows:

Permissible reduction = 812.8/919.3 = 0.884

Adjusted negative design moment = $721.9 \times 0.884 = 638.2$ ft-kips

Adjusted positive design moment = $197.3 \times 0.884 = 174.4$ ft-kips

$$M_o = 174.4 + \frac{638.2 + 638.2}{2} = 812.8$$
 ft-kips





ACI 318 allows the reduction of the moment values based on the previous procedure. Since the drop panels may cause gravity loads not to be uniform (Check limitation #5 and Figure 12), the moment values obtained from EFM will be used for comparison reasons.

b. Distribute factored moments to column and middle strips:

After the negative and positive moments have been determined for the slab-beam strip, the ACI code permits the distribution of the moments at critical sections to the column strips, beams (if any), and middle strips in accordance with the DDM. <u>ACI 318-14 (8.11.6.6)</u>

Table 2 - Distribution of factored moments								
		Slab-beam Strip	Slab-beam Strip Column Strip		Middle Strip			
		Moment (ft-kips)	Percent	Moment (ft-kips)	Percent	Moment (ft-kips)		
	Exterior Negative	246.5	100	246.5	0	0.0		
End Span	Positive	349.6	60	209.8	40	139.8		
	Interior Negative	695.9	75	521.9	25	174.0		
Interior Spon	Negative	623.4	75	467.6	25	155.9		
Interior Span	Positive	197.3	60	118.4	40	78.9		

Distribution of factored moments at critical sections is summarized in Table 2.

2.1.6. Flexural reinforcement requirements

a. Determine flexural reinforcement required for strip moments

The flexural reinforcement calculation for the column strip of end span – exterior negative location is provided below.

 $M_{\mu} = 246.5 \, \text{ft-kips}$

Use $d_{avg} = 12.75$ in.

To determine the area of steel, assumptions have to be made whether the section is tension or compression controlled, and regarding the distance between the resultant compression and tension forces along the slab section (*jd*). In this example, tension-controlled section will be assumed so the reduction factor φ is equal to 0.9, and *jd* will be taken equal to 0.95*d*. The assumptions will be verified once the area of steel in finalized. Assume $jd = 0.95 \times d = 12.11$ in.

Column strip width, $b = (30 \times 12)/2 = 180$ in.

Middle strip width, $b = 30 \times 12 - 180 = 180$ in.

$$A_s = \frac{M_u}{\varphi f_v jd} = \frac{246.5 \times 12000}{0.9 \times 60000 \times 12.11} = 4.52 \text{ in.}^2$$

Recalculate 'a' for the actual $A_s = 4.52 \text{ in.}^2 \rightarrow a = \frac{A_s f_y}{0.85 f'_c b} = \frac{5.09 \times 60000}{0.85 \times 5000 \times 180} = 0.355 \text{ in.}$



$$c = \frac{a}{\beta_1} = \frac{0.355}{0.85} = 0.417$$
 in.

$$\varepsilon_t = (\frac{0.003}{c})d_t - 0.003 = (\frac{0.003}{0.417}) \times 12.75 - 0.003 = 0.089 > 0.005$$

Therefore, the assumption that section is tension-controlled is valid.

$$A_s = \frac{M_u}{\varphi f_v (d - a/2)} = \frac{246.5 \times 12000}{0.9 \times 60000 \times (12.75 - 0.355/2)} = 4.357 \text{ in.}^2$$

The slab have two thicknesses in the column strip (14.25 in. for the slab with the drop panel and 10 in. for the slab without the drop panel).

The weighted slab thickness,
$$h_w = \frac{14.25 \times (30/3) + 10 \times (30/2 - 30/3)}{(30/3) + (30/2 - 30/3)} = 12.83$$
 in.
 $A_{s,\min} = 0.0018 \times 180 \times 12.83 = 4.157$ in.² < 4.357 in.² $ACI 318-14 (24.4.3.2)$
 $s_{\max} = 2h_w = 2 \times 12.83 = 25.66$ in. > 18 in. $ACI 318-14 (8.7.2.2)$
 $s_{\max} = 18$ in.

Provide 10 - #6 bars with $A_s = 4.40$ in.² and s = 180/10 = 18 in. $\le s_{max}$

Based on the procedure outlined above, values for all span locations are given in Table 3.

Location	M _u (ft-kips) 246.5	b (in.)	d (in.) Ene	A _s Req'd for flexure (in. ²)	Min A _s (in. ²)	Reinforcement Provided	A _s Prov. for flexure (in. ²)						
tterior Negative	246.5		En				nexure (III.)						
sterior Negative	246.5			d Span	End Span								
	= . 510	180	12.75	4.357	4.157	10-#6	4.40						
ositive	209.8	180	8.50	5.631	3.240	13-#6	5.72						
terior Negative	521.9	180	12.75	9.366	4.157	22-#6	9.68						
terior Negative	0.0	180	8.50	0.0	3.240	10-#6 * **	4.40						
ositive	139.8	180	8.50	3.719	3.240	10-#6 **	4.40						
terior Negative	174.0	180	8.50	4.649	3.240	11-#6	4.84						
Interior Span													
ositive	118.4	180	8.50	3.141	3.240	10-#6 * **	4.40						
ositive	78.9	180	8.50	2.083	3.240	10-#6 * **	4.40						
	sitive sitive sitive sitive sitive sitive rned by minimun	terior Negative 0.0 sitive 139.8 erior Negative 174.0 sitive 118.4 sitive 78.9 rned by minimum reinforcement	terior Negative 0.0 180 sitive 139.8 180 erior Negative 174.0 180 sitive 118.4 180 sitive 78.9 180 rned by minimum reinforcement.	B I I terior Negative 0.0 180 8.50 sitive 139.8 180 8.50 erior Negative 174.0 180 8.50 sitive 118.4 180 8.50 sitive 78.9 180 8.50 rned by minimum reinforcement. 8.50 180 8.50	B I	B I	B I						

** Number of bars governed by maximum allowable spacing.

b. Calculate additional slab reinforcement at columns for moment transfer between slab and column by flexure

The factored slab moment resisted by the column ($\gamma_f \ge M_{sc}$) shall be assumed to be transferred by flexure. Concentration of reinforcement over the column by closer spacing or additional reinforcement shall be used to resist this moment. The fraction of slab moment not calculated to be resisted by flexure shall be assumed to be resisted by eccentricity of shear. ACI 318-14 (8.4.2.3) ACI 318-14 (8.4.2.3.1)

Portion of the unbalanced moment transferred by flexure is $\gamma_f \ge M_{sc}$ Where

$$\gamma_f = \frac{1}{1 + (2/3) \times \sqrt{b_1/b_2}}$$

 b_1 = Dimension of the critical section b_0 measured in the direction of the span for which moments are determined in ACI 318, Chapter 8 (see Figure 13).

 b_2 = Dimension of the critical section b_0 measured in the direction perpendicular to b_1 in ACI 318, Chapter 8 (see Figure 13).

$$b_b$$
 = Effective slab width = $c_2 + 3 \times h$



c_{CD}

Ζ

 c_{AB}

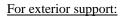
 \angle Edge of slab



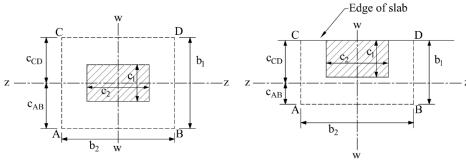


w

 b_2



d = h - cover - d/2 = 14.25 - 0.75 - 0.75/2 = 13.13 in. $b_1 = c_1 + d/2 = 20 + 13.13/2 = 26.56$ in. $b_2 = c_2 + d = 20 + 13.13 = 33.13$ in. $b_b = 20 + 3 \times 14.25 = 62.75$ in.



Edge of slab

D

Ŕ

 b_1

Z

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ACI 318-14 (8.4.2.3.2)

ACI 318-14 (8.4.2.3.3)

Critical shear perimeter for exterior column





$$\gamma_f = \frac{1}{1 + (2/3) \times \sqrt{26.56/33.13}} = 0.626$$

$$\gamma_f M_{sc} = 0.626 \times 331.7 = 207.7 \text{ ft-kips}$$

Using the same procedure in 2.1.7.a, the required area of steel:

$$A_s = 3.63 \text{ in.}^2$$

However, the area of steel provided to resist the flexural moment within the effective slab width b_b :

$$A_{s, provided} = 4.40 \times \frac{62.75}{180} = 1.534 \text{ in.}^2$$

Then, the required additional reinforcement at exterior column for moment transfer between slab and column:

 $A_{s.additional} = 3.63 - 1.534 = 2.096 \text{ in.}^2$

Provide 5 - #6 additional bars with $A_s = 2.20$ in.²

Based on the procedure outlined above, values for all supports are given in Table 4.

Table 4 - Additional Slab Reinforcement required for moment transfer between slab and column (EFM)									
Span Location		M _{sc} * (ft-kips)	γr	$\begin{array}{c} \gamma_f M_{sc} \\ (ft\text{-kips}) \end{array}$	Effective slab width, b _b (in.)	d (in.)	A _s req'd within b _b (in. ²)	A _s prov. For flexure within b _b (in. ²)	Add'l Reinf.
End Span									
C 1 . C	Exterior Negative	331.7	0.626	207.7	62.75	13.13	3.63	1.534	5-#6
Column Strip	Interior Negative	85.7	0.60	51.42	62.75	13.13	0.877	3.375	-
*M _{sc} is taken at the centerline of the support in Equivalent Frame Method solution.									

2.1.7. Factored moments in columns

The unbalanced moment from the slab-beams at the supports of the equivalent frame are distributed to the support columns above and below the slab-beam in proportion to the relative stiffness of the support columns. Referring to Figure 12, the unbalanced moment at the exterior and interior joints are:

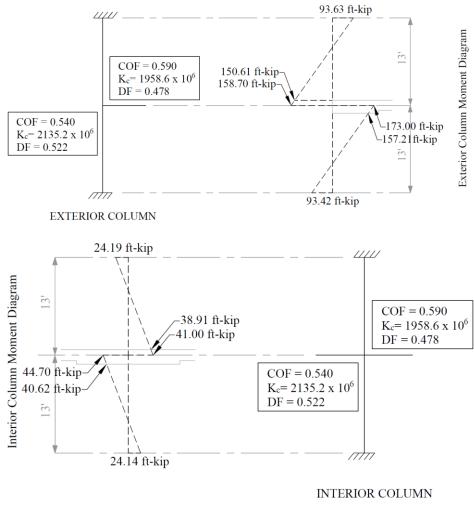
Exterior Joint = +331.7 ft-kips

Joint 2= -807.6 + 721.9 = -85.7 ft-kips

The stiffness and carry-over factors of the actual columns and the distribution of the unbalanced slab moments (M_{sc}) to the exterior and interior columns are shown in Figure 14.









In summary:

For Top column:	For Bottom column:
$M_{col,Exterior}$ = 150.61 ft-kips	$M_{col,Exterior}$ = 157.21 ft-kips
$M_{col,Interior} = 38.91$ ft-kips	$M_{col,Interior} = 40.62$ ft-kips
The moments determined above are combi	ned with the factored avial

The moments determined above are combined with the factored axial loads (for each story) and factored moments in the transverse direction for design of column sections. The moment values at the face of interior, exterior, and corner columns from the unbalanced moment values are shown in the following table.

Table 5 – Factored Moments in Columns			
M _u kips-ft	Column Location		
	Interior	Exterior	Corner
Mux	40.62	157.21	157.21
Muy	40.62	40.62	157.21

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3. Design of Columns by spColumn

This section includes the design of interior, edge, and corner columns using <u>spColumn</u> software. The preliminary dimensions for these columns were calculated previously in section one. The reduction of live load per <u>ASCE</u> <u>7-10</u> will be ignored in this example. However, the detailed procedure to calculate the reduced live loads is explained in the "wide-Module Joist System" example.

3.1. Determination of factored loads

Interior Column:

Assume 5 story building

Tributary area for interior column for live load, superimposed dead load, and self-weight of the slab is

 $A_{Tributary} = 30 \times 30 = 900 \text{ ft}^2$

Tributary area for interior column for self-weight of additional slab thickness due to the presence of the drop panel is

$$A_{Tributary} = 10 \times 10 = 100 \text{ ft}^2$$

Assuming five story building

 $P_{\mu} = n \times q_{\mu} \times A_{Tributary} = 5 \times (0.270 \times 900 + 0.0638 \times 100) = 1247$ kips

 $M_{u,x} = 40.62$ ft-kips (see the previous Table)

 $M_{u,y} = 40.62$ ft-kips (see the previous Table)

Edge (Exterior) Column:

Tributary area for interior column for live load, superimposed dead load, and self-weight of the slab is

$$A_{Tributary} = \left(\frac{30}{2} + \frac{20/2}{12}\right) \times 30 = 475 \text{ ft}^2$$

Tributary area for interior column for self-weight of additional slab thickness due to the presence of the drop panel is

$$A_{Tributary} = \left(\frac{10}{2} + \frac{20/2}{12}\right) \times 10 = 58.33 \text{ ft}^2$$

 $P_u = n \times q_u \times A_{Tributary} = 5 \times (0.270 \times 475 + 0.0638 \times 58.33) = 660$ kips

 $M_{u,x} = 157.21$ ft-kips (see the previous Table)

 $M_{u,y} = 40.62$ ft-kips (see the previous Table)

Corner Column:

Tributary area for interior column for live load, superimposed dead load, and self-weight of the slab is

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$$A_{Tributary} = \left(\frac{30}{2} + \frac{20/2}{12}\right) \times \left(\frac{30}{2} + \frac{20/2}{12}\right) = 251 \, \text{ft}^2$$

Tributary area for interior column for self-weight of additional slab thickness due to the presence of the drop panel is

$$A_{Tributary} = \left(\frac{10}{2} + \frac{20/2}{12}\right) \times \left(\frac{10}{2} + \frac{20/2}{12}\right) = 34.03 \text{ ft}^2$$
$$P_u = n \times q_u \times A_{Tributary} = 5 \times (0.270 \times 251 + 0.0638 \times 34.03) = 350 \text{ kips}$$

 $M_{u,x} = 157.21$ ft-kips (see the previous Table)

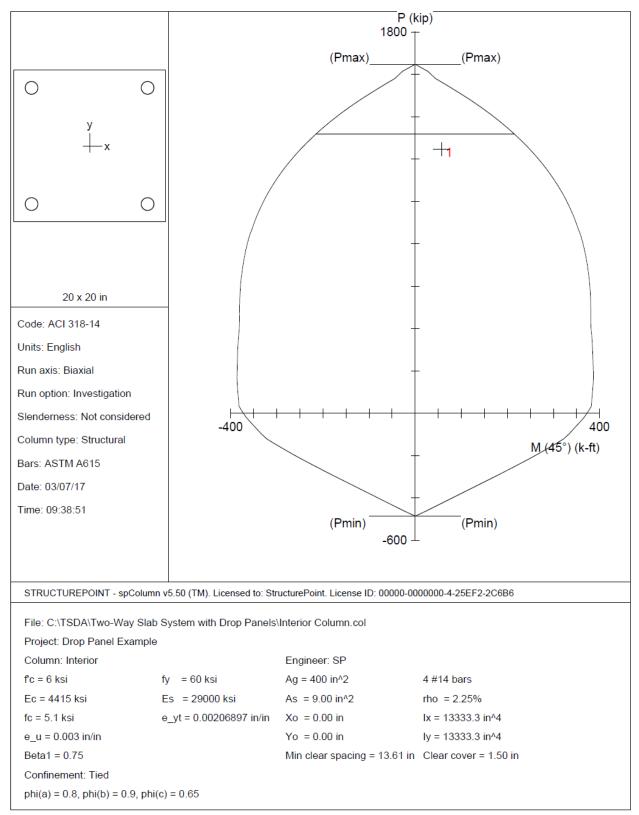
 $M_{u,y} = 157.21$ ft-kips (see the previous Table)

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3.2. Moment Interaction Diagram

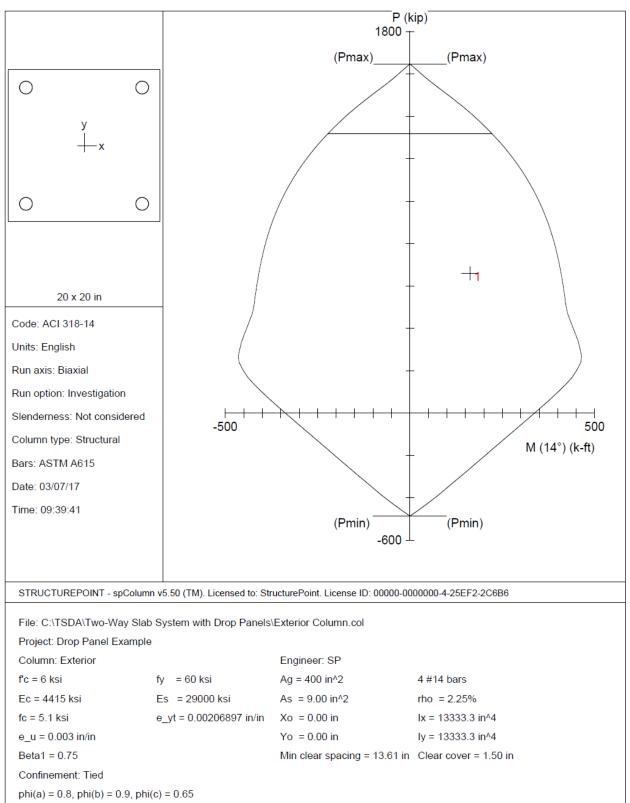
Interior Column:







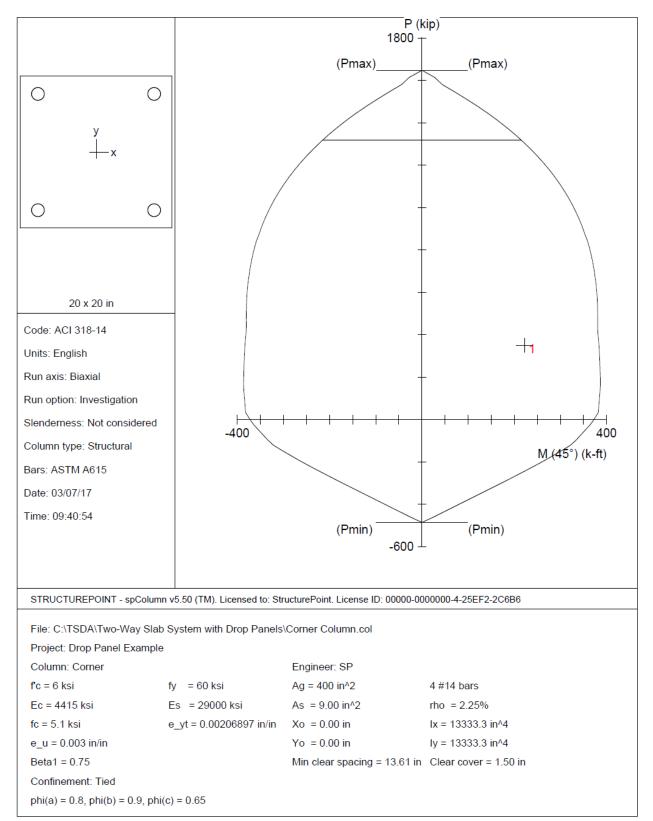
Edge Column:







Corner Column:





4. Shear Strength

Shear strength of the slab in the vicinity of columns/supports includes an evaluation of one-way shear (beam action) and two-way shear (punching) in accordance with ACI 318 Chapter 22.

4.1. One-Way (Beam action) Shear Strength

ACI 318-14 (22.5)

One-way shear is critical at a distance d from the face of the column as shown in Figure 3. Figures 15 and 16 show the factored shear forces (V_u) at the critical sections around each column and each drop panel, respectively. In members without shear reinforcement, the design shear capacity of the section equals to the design shear capacity of the concrete:

$$\varphi V_n = \varphi V_c + \varphi V_s = \varphi V_c$$
, $(\varphi V_s = 0)$
ACI 318-14 (Eq. 22.5.1.1)

Where:

$$\varphi V_c = \varphi 2\lambda \sqrt{f'_c b_w} d \qquad \underline{ACI 318-14 (Eq. 22.5.5.1)}$$

4.1.1. At distance *d* from the supporting column

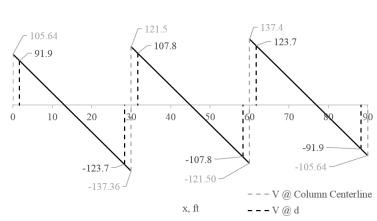
$$h_{weighted} = \frac{14.25 \times 30/6 + 10 \times (30 - 30/6)}{30} = 11.42 \text{ in.}$$

$$d_w = 11.42 - 0.75 - 0.75/2 = 10.29 \text{ in.}$$

 $\lambda = 1$ for normal weight concrete

$$\varphi V_c = 0.75 \times 2 \times 1.0 \times \frac{\sqrt{5000}}{1000} \times (30 \times 12) \times 10.29 = 392.91 \text{ kips}$$

Because $\varphi V_c \ge V_u$ at all the critical sections, the slab has adequate one-way shear strength.



Shear Diagram (kips)

Figure 15 – One-way shear at critical sections (at distance d from the face of the supporting column)



4.1.2. At the face of the drop panel

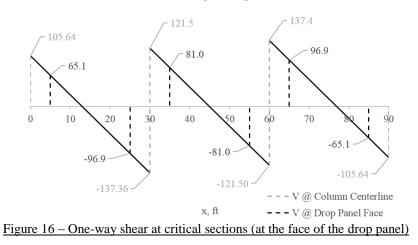
- h = 10 in. *in*.
- d = 10 0.75 0.75 / 2 = 8.88 in.

 $\lambda = 1$ for normal weight concrete

$$\varphi V_c = 0.75 \times 2 \times 1.0 \times \frac{\sqrt{5000}}{1000} \times (30 \times 12) \times 8.88 = 339.1 \text{ kips}$$

Because $\phi V_c \ge V_u$ at all the critical sections, the slab has adequate one-way shear strength.

Shear Diagram (kips)







4.2.1. Around the columns faces

Two-way shear is critical on a rectangular section located at d/2 away from the face of the column as shown in Figure 13.

a. Exterior column:

The factored shear force (V_u) in the critical section is computed as the reaction at the centroid of the critical section minus the self-weight and any superimposed surface dead and live load acting within the critical section (d/2 away from column face).

$$V_u = V - q_u (b_1 \times b_2) = 105.64 - 0.334 \left(\frac{26.56 \times 33.13}{144}\right) = 103.60 \text{ kips}$$

The factored unbalanced moment used for shear transfer, M_{unb} , is computed as the sum of the joint moments to the left and right. Moment of the vertical reaction with respect to the centroid of the critical section is also taken into account.

$$M_{unb} = M - V_u \left(b_1 - c_{AB} - c_1 / 2 \right) = 331.7 - 103.60 \left(\frac{26.56 - 8.18 - 20 / 2}{12} \right) = 259 \text{ ft-kips}$$

For the exterior column in Figure 13, the location of the centroidal axis z-z is:

$$c_{AB} = \frac{moment \ of \ area \ of \ the \ sides \ about \ AB}{area \ of \ the \ sides} = \frac{2(26.56 \times 13.13 \times 26.56 / 2)}{2 \times 26.56 \times 13.13 + 33.13 \times 13.13} = 8.18 \text{ in}$$

The polar moment J_c of the shear perimeter is:

$$J_{c} = 2\left(\frac{b_{1}d^{3}}{12} + \frac{db_{1}^{3}}{12} + (b_{1}d)\left(\frac{b_{1}}{2} - c_{AB}\right)^{2}\right) + b_{2}dc_{AB}^{2}$$
$$J_{c} = 2\left(\frac{26.56 \times 13.13^{3}}{12} + \frac{13.13 \times 26.56^{3}}{12} + (26.56 \times 13.13)\left(\frac{26.56}{2} - 8.18\right)^{2}\right) + 33.13 \times 13.13 \times 8.18^{2}$$
$$J_{c} = 98,315 \text{ in.}^{4}$$

 $\gamma_v = 1 - \gamma_f = 1 - 0.626 = 0.374$ ACI 318-14 (Eq. 8.4.4.2.2)

The length of the critical perimeter for the exterior column:

$$b_o = 2 \times 26.56 + 33.13 = 86.26$$
 in.

The two-way shear stress (v_u) can then be calculated as:



$$\begin{aligned} v_u &= \frac{V_u}{b_o \times d} + \frac{\gamma \frac{M}{v} \frac{M_{unb} c_{AB}}{J_c}}{J_c} \\ v_u &= \frac{103.60 \times 1000}{86.26 \times 13.13} + \frac{0.374 \times (259 \times 12 \times 1000) \times 8.18}{98,315} = 188.3 \text{ psi} \\ v_c &= min \bigg[4\lambda \sqrt{f_c} , \bigg(2 + \frac{4}{\beta} \bigg) \lambda \sqrt{f_c} , \bigg(\frac{a_s d}{b_o} + 2 \bigg) \lambda \sqrt{f_c} \bigg] \\ v_c &= min \bigg[4 \times 1 \times \sqrt{5000} , \bigg(2 + \frac{4}{1} \bigg) \times 1 \times \sqrt{5000} , \bigg(\frac{30 \times 13.13}{86.26} + 2 \bigg) \times 1 \times \sqrt{5000} \bigg] \\ v_c &= min \bigg[282.8, 424.3, 464.3 \bigg] \, psi = 282.8 \text{ psi} \\ \varphi v_c &= 0.75 \times 282.8 = 212.1 \text{ psi} \end{aligned}$$

Since $\varphi v_c \ge v_u$ at the critical section, the slab has adequate two-way shear strength at this joint.

b. Interior column:

$$V_u = V - q_u \left(b_1 \times b_2 \right) = 137.36 + 121.5 - 0.334 \left(\frac{33.13 \times 33.13}{144} \right) = 256.35 \text{ kips}$$
$$M_{unb} = M - V_u \left(b_1 - c_{AB} - c_1 / 2 \right) = 807.6 - 721.9 - 256.31 \text{ (0)} = 85.70 \text{ ft-kips}$$

For the interior column in Figure 13, the location of the centroidal axis z-z is:

$$c_{AB} = \frac{b}{2} = \frac{33.13}{2} = 16.57$$
 in.

The polar moment J_c of the shear perimeter is:

$$\begin{split} J_{c} &= 2 \Biggl(\frac{b_{d}^{3}}{12} + \frac{db_{1}^{3}}{12} + \left(b_{1}d \right) \left(\frac{b_{1}}{2} - c_{AB} \right)^{2} \Biggr) + 2b_{2}dc_{AB}^{2} \\ J_{c} &= 2 \Biggl(\frac{33.13 \times 13.13^{3}}{12} + \frac{13.13 \times 33.13^{3}}{12} + \left(33.13 \times 13.13 \right) \left(\frac{33.13}{2} - 16.57 \right)^{2} \Biggr) + 2 \times 33.13 \times 13.13 \times 16.57^{2} \\ J_{c} &= 330,800 \text{ in.}^{4} \\ \gamma_{v} &= 1 - \gamma_{f} = 1 - 0.600 = 0.400 \end{aligned}$$

The length of the critical perimeter for the interior column:



 $b_o = 2 \times (33.13 + 33.13) = 132.52$ in.

The two-way shear stress (v_u) can then be calculated as:

$$\begin{aligned} v_{u} &= \frac{V_{u}}{b_{o} \times d} + \frac{\gamma_{v} M_{unb} c_{AB}}{J_{c}} & \underline{ACI 318-14 (R.8.4.4.2.3)} \\ v_{u} &= \frac{256.31 \times 1000}{132.52 \times 13.13} + \frac{0.400 \times (85.70 \times 12 \times 1000) \times 16.57}{330,800} = 167.9 \text{ psi} \\ v_{c} &= min \left[4\lambda \sqrt{f_{c}}, \left(2 + \frac{4}{\beta} \right) \lambda \sqrt{f_{c}}, \left(\frac{\alpha_{s} d}{b_{o}} + 2 \right) \lambda \sqrt{f_{c}} \right] & \underline{ACI 318-14 (Table 22.6.5.2)} \\ v_{c} &= min \left[4 \times 1 \times \sqrt{5000}, \left(2 + \frac{4}{1} \right) \times 1 \times \sqrt{5000}, \left(\frac{40 \times 13.13}{132.52} + 2 \right) \times 1 \times \sqrt{5000} \right] \\ v_{c} &= min \left[282.8, 424.3, 421.7 \right] \text{ psi} = 282.8 \text{ psi} \\ \varphi v_{c} &= 0.75 \times 282.8 = 212.1 \text{ psi} \end{aligned}$$

Since $\varphi v_c \ge v_{\mu}$ at the critical section, the slab has adequate two-way shear strength at this joint.

c. Corner column:

In this example, interior equivalent frame strip was selected where it only have exterior and interior supports (no corner supports are included in this strip). However, the two-way shear strength of corner supports usually governs. Thus, the two-way shear strength for the corner column in this example will be checked for educational purposes. Same procedure is used to find the reaction and factored unbalanced moment used for shear transfer at the centroid of the critical section for the corner support for the exterior equivalent frame strip.

$$V_{u} = V - q_{u} (b_{l} \times b_{2}) = 61.93 - 0.334 \left(\frac{26.56 \times 26.56}{144}\right) = 60.29 \text{ kips}$$
$$M_{unb} = M - V_{u} (b_{l} - c_{AB} - c_{1}/2) = 189.12 - 60.29 \left(\frac{26.56 - 6.64 - 20/2}{12}\right) = 139.26 \text{ ft-kips}$$

For the interior column in Figure 13, the location of the centroidal axis z-z is:

$$c_{AB} = \frac{\text{moment of area of the sides about AB}}{\text{area of the sides}} = \frac{(26.56 \times 13.13 \times 26.56/2)}{26.56 \times 13.13 + 26.56 \times 13.13} = 6.64 \text{ in. in}$$

The polar moment J_c of the shear perimeter is:

$$J_{c} = \left(\frac{b_{1}d^{3}}{12} + \frac{db_{1}^{3}}{12} + (b_{1}d)\left(\frac{b_{1}}{2} - c_{AB}\right)^{2}\right) + b_{2}dc_{AB}^{2}$$



$$J_{c} = \left(\frac{26.56 \times 13.13^{3}}{12} + \frac{13.13 \times 26.56^{3}}{12} + (26.56 \times 13.13) \left(\frac{26.56}{2} - 6.64\right)^{2}\right) + 26.56 \times 13.13 \times 6.64^{2}$$

$$J_{c} = 56,292 \text{ in.}^{4}$$

$$\gamma_{v} = 1 - \gamma_{f} = 1 - 0.600 = 0.400$$

$$\underline{ACI 318-14 (Eq. 8.4.4.2.2)}$$

The length of the critical perimeter for the corner column:

 $b_o = 26.56 + 26.56 = 53.13$ in.

The two-way shear stress (v_u) can then be calculated as:

$$\begin{aligned} v_u &= \frac{V_u}{b_o \times d} + \frac{\gamma M_{unb} c_{AB}}{J_c} \\ v_u &= \frac{60.29 \times 1000}{53.13 \times 13.13} + \frac{0.400 \times (139.26 \times 12 \times 1000) \times 6.64}{56,292} = 165.3 \text{ psi} \\ v_c &= min \bigg[4\lambda \sqrt{f_c} , \bigg(2 + \frac{4}{\beta} \bigg) \lambda \sqrt{f_c} , \bigg(\frac{\alpha_s d}{b_o} + 2 \bigg) \lambda \sqrt{f_c} \bigg] \\ v_c &= min \bigg[4 \times 1 \times \sqrt{5000} , \bigg(2 + \frac{4}{1} \bigg) \times 1 \times \sqrt{5000} , \bigg(\frac{20 \times 13.13}{53.13} + 2 \bigg) \times 1 \times \sqrt{5000} \bigg] \\ v_c &= min \bigg[282.8, 424.3, 490.9 \bigg] \text{ psi} = 282.8 \text{ psi} \\ \varphi v_c &= 0.75 \times 282.8 = 212.1 \text{ psi} \end{aligned}$$

Since $\varphi v_c \ge v_u$ at the critical section, the slab has adequate two-way shear strength at this joint.

4.2.2. Around drop panels

Two-way shear is critical on a rectangular section located at d/2 away from the face of the drop panel.

a. Exterior drop panel:

$$V_{u} = V - q_{u1}A_{1} - q_{u2}A_{2} = 105.64 - 0.334 \left(\frac{70 \times 120}{144}\right) - 0.270 \left(\frac{74.44 \times 128.88 - 70 \times 120}{144}\right) = 83.92 \text{ kips}$$
$$M_{unb} = M - V_{u} \left(b_{1} - c_{AB} - c_{1}/2\right) = 331.7 - 83.92 \left(\frac{74.44 - 19.95 - 20/2}{12}\right) = 20.57 \text{ ft-kips}$$

For the exterior drop panel, the location of the centroidal axis z-z is:





$$c_{AB} = \frac{moment of area of the sides about AB}{area of the sides} = \frac{2(74.44 \times 8.88 \times 74.44/2)}{2 \times 74.44 \times 8.88 + 128.88 \times 8.88} = 19.95 \text{ in}.$$

The polar moment J_c of the shear perimeter is:

$$\begin{split} J_{c} &= 2 \Biggl(\frac{b_{1}d^{3}}{12} + \frac{db_{1}^{3}}{12} + \left(b_{1}d \right) \left(\frac{b_{1}}{2} - c_{AB} \right)^{2} \Biggr) + b_{2}dc_{AB}^{2} \\ J_{c} &= 2 \Biggl(\frac{74.44 \times 8.88^{3}}{12} + \frac{8.88 \times 74.44^{3}}{12} + \left(74.44 \times 8.88 \right) \left(\frac{74.44}{2} - 19.95 \right)^{2} \Biggr) + 128.88 \times 8.88 \times 19.95^{2} \\ J_{c} &= 1,468,983 \text{ in.}^{4} \\ \gamma_{v} &= 1 - \gamma_{f} = 1 - 0.664 = 0.336 \end{aligned}$$

The length of the critical perimeter for the exterior drop panel:

$$b_o = 2 \times 74.44 + 128.88 = 277.76$$
 in.

The two-way shear stress (v_u) can then be calculated as:

$$v_{u} = \frac{V_{u}}{b_{o} \times d} + \frac{\gamma M_{unb} c_{AB}}{J_{c}}$$

$$ACI 318-14 (R.8.4.4.2.3)$$

$$v_{u} = \frac{83.92 \times 1000}{2777.76 \times 8.88} + \frac{0.336 \times (20.57 \times 12 \times 1000) \times 19.95}{1,468,983} = 35.2 \text{ psi}$$

$$v_{c} = min \left[4\lambda \sqrt{f_{c}}, \left(2 + \frac{4}{\beta}\right) \lambda \sqrt{f_{c}}, \left(\frac{\alpha_{s}d}{b_{o}} + 2\right) \lambda \sqrt{f_{c}} \right]$$

$$ACI 318-14 (Table 22.6.5.2)$$

$$v_{c} = min \left[4 \times 1 \times \sqrt{5000}, \left(2 + \frac{4}{1}\right) \times 1 \times \sqrt{5000}, \left(\frac{30 \times 8.88}{2777.76} + 2\right) \times 1 \times \sqrt{5000} \right]$$

$$v_{c} = min \left[282.8, 424.3, 209.2 \right] \text{ psi} = 209.2 \text{ psi}$$

$$\varphi v_{c} = 0.75 \times 209.2 = 156.9 \text{ psi}$$

Since $\varphi v_c \ge v_u$ at the critical section, the slab has adequate two-way shear strength around this drop panel.



b. Interior drop panel:

$$V_{u} = V - q_{u1}A_{1} - q_{u2}A_{2}$$

$$V_{u} = 137.36 + 121.5 - 0.334 \left(\frac{120 \times 120}{144}\right) - 0.270 \left(\frac{128.88 \times 128.88 - 120 \times 120}{144}\right) = 220.37 \text{ kips}$$

$$M_{unb} = M - V_{u} \left(b_{1} - c_{AB} - c_{1}/2\right) = 807.6 - 721.9 - 220.37 \text{ (0)} = 85.70 \text{ ft-kips}$$

For the interior drop panel, the location of the centroidal axis z-z is:

$$c_{AB} = \frac{b_1}{2} = \frac{128.88}{2} = 64.44$$
 in.

The polar moment J_c of the shear perimeter is:

$$\begin{split} J_{c} &= 2 \Biggl(\frac{b_{1}^{d}}{12} + \frac{db_{1}^{3}}{12} + \binom{b_{1}}{12} + \binom{b_{1}}{2} - \binom{b_{1}}{2} - c_{AB}^{2} \Biggr)^{2} \Biggr) + 2b_{2}dc_{AB}^{2} \\ J_{c} &= 2 \Biggl(\frac{128.88 \times 8.88^{3}}{12} + \frac{128.88 \times 8.88^{3}}{12} + (128.88 \times 8.88) \left(\frac{128.88}{2} - 64.44 \right)^{2} \Biggr) + 2 \times 128.88 \times 8.88 \times 64.44^{2} \\ J_{c} &= 12,688,007 \text{ in.}^{4} \\ \gamma_{v} &= 1 - \gamma_{f} = 1 - 0.600 = 0.400 \end{aligned}$$

The length of the critical perimeter for the interior drop panel:

$$b_o = 2 \times (128.88 + 128.88) = 515.52$$
 in.

The two-way shear stress (v_u) can then be calculated as:

$$\begin{aligned} v_u &= \frac{V_u}{b_o \times d} + \frac{\gamma_v M_{unb} c_{AB}}{J_c} \\ v_u &= \frac{220.37 \times 1000}{515.52 \times 8.88} + \frac{0.400 \times (85.70 \times 12 \times 1000) \times 64.44}{12,688,007} = 50.2 \text{ psi} \\ v_c &= min \bigg[4\lambda \sqrt{f_c}, \bigg(2 + \frac{4}{\beta} \bigg) \lambda \sqrt{f_c}, \bigg(\frac{\alpha_s d}{b_o} + 2 \bigg) \lambda \sqrt{f_c} \bigg] \\ v_c &= min \bigg[4 \times 1 \times \sqrt{5000}, \bigg(2 + \frac{4}{1} \bigg) \times 1 \times \sqrt{5000}, \bigg(\frac{40 \times 8.88}{515.52} + 2 \bigg) \times 1 \times \sqrt{5000} \bigg] \end{aligned}$$



- $v_c = min[282.8, 424.3, 190.1]$ psi = 190.1 psi
- $\varphi v_c = 0.75 \times 190.1 = 142.6 \text{ psi}$

Since $\varphi v_c \ge v_u$ at the critical section, the slab has adequate two-way shear strength around this drop panel.

c. Corner drop panel:

$$V_{u} = V - q_{ul}A_{l} - q_{u2}A_{2}$$

$$V_{u} = 61.93 - 0.334 \left(\frac{70 \times 70}{144}\right) - 0.270 \left(\frac{74.44 \times 74.44 - 70 \times 70}{144}\right) = 49.36 \text{ kips}$$

$$M_{unb} = M - V_{u} \left(b_{l} - c_{AB} - c_{1}/2\right) = 189.12 - 49.36 \left(\frac{74.44 - 18.61 - 20/2}{12}\right) = 0.60 \text{ ft-kips}$$

For the corner drop panel, the location of the centroidal axis z-z is:

$$c_{AB} = \frac{moment of area of the sides about AB}{area of the sides} = \frac{(74.44 \times 8.88 \times 74.44/2)}{74.44 \times 8.88 + 74.44 \times 8.88} = 18.61 \text{ in.}$$

The polar moment J_c of the shear perimeter is:

$$J_{c} = \left(\frac{b_{1}d^{3}}{12} + \frac{db_{1}^{3}}{12} + (b_{1}d)\left(\frac{b_{1}}{2} - c_{AB}\right)^{2}\right) + b_{2}dc_{AB}^{2}$$

$$J_{c} = \left(\frac{74.44 \times 8.88^{3}}{12} + \frac{8.88 \times 74.44^{3}}{12} + (74.44 \times 8.88)\left(\frac{74.44}{2} - 18.61\right)^{2}\right) + 74.44 \times 8.88 \times 18.61^{2}$$

$$J_{c} = 767,460 \text{ in.}^{4}$$

$$\gamma_{v} = 1 - \gamma_{f} = 1 - 0.600 = 0.400$$
ACI 318-14 (Eq. 8.4.4.2.2)

The length of the critical perimeter for the corner drop panel:

$$b_o = 74.44 + 74.44 = 148.88$$
 in.

The two-way shear stress (v_u) can then be calculated as:

$$v_{u} = \frac{V_{u}}{b_{o} \times d} + \frac{\gamma_{v} M_{unb} c_{AB}}{J_{c}}$$

$$v_{u} = \frac{49.36 \times 1000}{148.88 \times 8.88} + \frac{0.400 \times (0.60 \times 12 \times 1000) \times 18.61}{767,460} = 37.4 \text{ psi}$$





$$v_{c} = min \left[4\lambda \sqrt{f_{c}}, \left(2 + \frac{4}{\beta}\right) \lambda \sqrt{f_{c}}, \left(\frac{a_{s}d}{b_{o}} + 2\right) \lambda \sqrt{f_{c}} \right]$$

$$v_{c} = min \left[4 \times 1 \times \sqrt{5000}, \left(2 + \frac{4}{1}\right) \times 1 \times \sqrt{5000}, \left(\frac{20 \times 8.88}{148.88} + 2\right) \times 1 \times \sqrt{5000} \right]$$

$$v_{c} = min \left[282.8, 424.3, 225.8 \right] \text{ psi} = 225.8 \text{ psi}$$

$$\varphi v_{c} = 0.75 \times 225.8 = 169.3 \text{ psi}$$

Since $\varphi v_c \ge v_u$ at the critical section, the slab has adequate two-way shear strength around this drop panel.



5. Serviceability Requirements (Deflection Check)

Since the slab thickness was selected below the minimum slab thickness tables in ACI 318-14, the deflection calculations of immediate and time-dependent deflections are required and shown below including a comparison with spSlab model results.

5.1. Immediate (Instantaneous) Deflections

The calculation of deflections for two-way slabs is challenging even if linear elastic behavior can be assumed. Elastic analysis for three service load levels $(D, D + L_{sustained}, D + L_{Full})$ is used to obtain immediate deflections of the two-way slab in this example. However, other procedures may be used if they result in predictions of deflection in reasonable agreement with the results of comprehensive tests. The effective moment of inertia (I_e) is used to account for the cracking effect on the flexural stiffness of the slab. I_e for uncracked section $(M_{cr} > M_a)$ is equal to I_g . When the section is cracked $(M_{cr} < M_a)$, then the following equation should be used:

$$I_e = \left(\frac{M_{cr}}{M_a}\right)^3 I_g + \left[1 - \left(\frac{M_{cr}}{M_a}\right)^3\right] I_{cr} \le I_g \qquad \underline{ACI 318-14 (Eq. 24.2.3.5a)}$$

Where:

 M_a = Maximum moment in member due to service loads at stage deflection is calculated.

The values of the maximum moments for the three service load levels are calculated from structural analysis as shown previously in this document. These moments are shown in Figure 17.





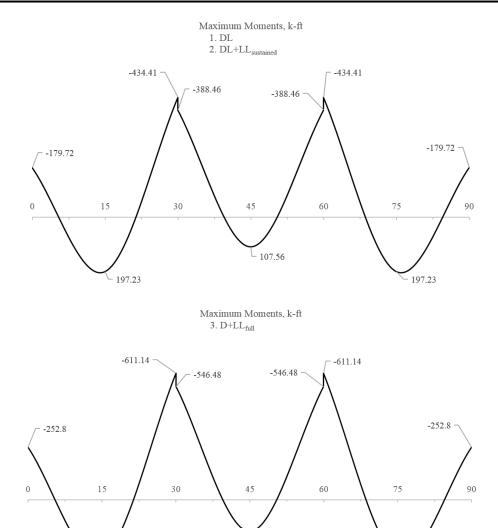


Figure 17 – Maximum Moments for the Three Service Load Levels

- 152.03

278.14

For positive moment (midspan) section:

- 278.14

 M_{cr} = Cracking moment.

$$M_{cr} = \frac{f_r I_g}{y_t} = \frac{530.33 \times 30000}{5} \times \frac{1}{12 \times 1000} = 265.17 \text{ ft-kips}$$
 ACI 318-14 (Eq. 24.2.3.5b)

 f_r = Modulus of rapture of concrete.

$$f_r = 7.5\lambda \sqrt{f_c} = 7.5 \times 1.0 \times \sqrt{5000} = 530.33 \text{ psi}$$
 ACI 318-14 (Eq. 19.2.3.1)

 I_{g} = Moment of inertia of the gross uncracked concrete section.



$$I_g = \frac{l_2 h^3}{12} = \frac{(30 \times 12) (10)^3}{12} = 30000 \text{ in.}^2$$

 y_t = Distance from centroidal axis of gross section, neglecting reinforcement, to tension face, in.

$$y_t = \frac{h}{2} = \frac{10}{2} = 5$$
 in.

 I_{cr} = Moment of inertia of the cracked section transformed to concrete. <u>PCA N</u>

PCA Notes on ACI 318-11 (9.5.2.2)

As calculated previously, the positive reinforcement for the end span frame strip is 23 #6 bars located at 1.125 in. along the section from the bottom of the slab. Two of these bars are not continuous and will be excluded from the calculation of I_{cr} . Figure 18 shows all the parameters needed to calculate the moment of inertia of the cracked section transformed to concrete at midspan.

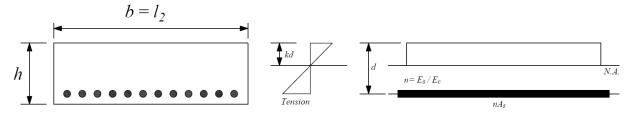


Figure 18 – Cracked Transformed Section (positive moment section)

 E_{cs} = Modulus of elasticity of slab concrete.

$$E_{cs} = w_c^{1.5} 33\sqrt{f_c'} = 150^{1.5} \times 33 \times \sqrt{5000} = 4287 \times 10^3 \text{ psi}$$

$$n = \frac{E_s}{E_{cs}} = \frac{29000000}{4287000} = 6.76$$

$$\frac{PCA \text{ Notes on ACI 318-11 (Table 10-2)}}{B = \frac{b}{nA_s}} = \frac{30 \times 12}{6.76 \times (21 \times 0.44)} = 5.76 \text{ in.}^{-1}$$

$$\frac{PCA \text{ Notes on ACI 318-11 (Table 10-2)}}{5.76}$$

$$\frac{PCA \text{ Notes on ACI 318-11 (Table 10-2)}}{B = 1.59 \text{ in.}}$$

$$\frac{PCA \text{ Notes on ACI 318-11 (Table 10-2)}}{B = \frac{\sqrt{224B+1}-1}{B}} = \frac{\sqrt{2 \times 8.88 \times 5.76+1}-1}{5.76} = 1.59 \text{ in.}$$

$$\frac{PCA \text{ Notes on ACI 318-11 (Table 10-2)}}{B = 1.59 \text{ in.}}$$

$$\frac{PCA \text{ Notes on ACI 318-11 (Table 10-2)}}{B = 1.59 \text{ in.}}$$

$$\frac{PCA \text{ Notes on ACI 318-11 (Table 10-2)}}{B = 1.59 \text{ in.}}$$

For negative moment section (near the interior support of the end span):

The negative reinforcement for the end span frame strip near the interior support is 32 #6 bars located at 1.125 in. along the section from the top of the slab.





$$M_{cr} = \frac{f_r I_g}{y_t} = \frac{530.33 \times 53445}{5.88} \times \frac{1}{12 \times 1000} = 401.42 \text{ ft-kips} \qquad \underline{ACI 318-14 (Eq. 24.2.3.5b)}$$

$$f_r = 7.5\lambda \sqrt{f_c} = 7.5 \times 1.0 \times \sqrt{5000} = 530.33 \text{ psi}$$

$$I_g = 53445 \text{ in.}^2$$

$$y_t = 5.88 \text{ in.}$$

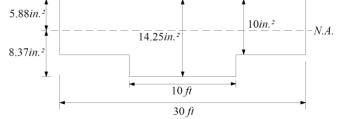


Figure $19 - I_g$ calculations for slab section near support

$$E_{cs} = w_c^{1.5} 33\sqrt{f_c'} = 150^{1.5} \times 33 \times \sqrt{5000} = 4287 \times 10^3 \text{ psi}$$

$$n = \frac{E_s}{E_{cs}} = \frac{29000000}{4287000} = 6.76$$

$$PCA \text{ Notes on ACI 318-11 (Table 10-2)}$$

$$B = \frac{b_b}{nA_s} = \frac{10 \times 12}{6.76 \times (32 \times 0.44)} = 1.26 \text{ in.}^{-1}$$

$$PCA \text{ Notes on ACI 318-11 (Table 10-2)}$$

$$kd = \frac{\sqrt{2dB+1}-1}{B} = \frac{\sqrt{2 \times 13.13 \times 1.26 + 1}-1}{1.26} = 3.84 \text{ in.}$$

$$PCA \text{ Notes on ACI 318-11 (Table 10-2)}$$

$$I_{cr} = \frac{b_b(kd)^3}{3} + nA_s(d-kd)^2$$

$$PCA \text{ Notes on ACI 318-11 (Table 10-2)}$$

$$I_{cr} = \frac{10 \times 12 \times (3.84)^3}{3} + 6.76 \times (32 \times 0.44) (13.13 - 3.84)^2 = 10471 \text{ in.}^4$$





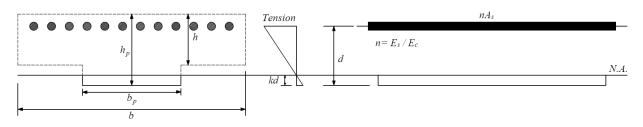


Figure 20 - Cracked Transformed Section (negative moment section)

The effective moment of inertia procedure described in the Code is considered sufficiently accurate to estimate deflections. The effective moment of inertia, I_e , was developed to provide a transition between the upper and lower bounds of I_g and I_{cr} as a function of the ratio M_{cr}/M_a . For conventionally reinforced (nonprestressed) members, the effective moment of inertia, I_e , shall be calculated by Eq. (24.2.3.5a) unless obtained by a more comprehensive analysis.

 I_e shall be permitted to be taken as the value obtained from Eq. (24.2.3.5a) at midspan for simple and continuous spans, and at the support for cantilevers. ACI 318-14 (24.2.3.7)

For continuous one-way slabs and beams. I_e shall be permitted to be taken as the average of values obtained from Eq. (24.2.3.5a) for the critical positive and negative moment sections. <u>ACI 318-14 (24.2.3.6)</u>

For the middle span (span with two ends continuous) with service load level $(D+LL_{full})$:

$$I_e^- = \left(\frac{M_{cr}}{M_a}\right)^3 I_g + \left[1 - \left(\frac{M_{cr}}{M_a}\right)^3\right] I_{cr} \text{, since } M_{cr} = 401.4 \text{ ft-kips} < M_a = 546.5 \text{ ft-kips}$$

ACI 318-14 (24.2.3.5a)

Where I_e^{-} is the effective moment of inertia for the critical negative moment section (near the support).

$$I_{e}^{-} = \left(\frac{401.4}{546.5}\right)^{3} \times 53445 + \left[1 - \left(\frac{401.4}{546.5}\right)^{3}\right] \times 10471 = 27503 \text{ in.}^{4}$$
$$I_{e}^{+} = I_{e}^{-} = 30000 \text{ in.}^{4} \text{ , since } M_{cr} = 265.17 \text{ ft-kips} > M_{a} = 152.03 \text{ ft-kips}$$

Where I_{e^+} is the effective moment of inertia for the critical positive moment section (midspan).



Since midspan stiffness (including the effect of cracking) has a dominant effect on deflections, midspan section is heavily represented in calculation of I_e and this is considered satisfactory in approximate deflection calculations. Both the midspan stiffness (I_e^+) and averaged span stiffness ($I_{e,avg}$) can be used in the calculation of immediate (instantaneous) deflection.

The averaged effective moment of inertia $(I_{e,avg})$ is given by:

$$I_{e,avg} = 0.70 I_e^+ + 0.15 \left(I_{e,l}^- + I_{e,r}^- \right)$$
 for interior span
PCA Notes on ACI 318-11 (9.5.2.4(2))

 $I_{e,avg} = 0.85 I_e^+ + 0.15 I_e^-$ for end span <u>PCA Notes on ACI 318-11 (9.5.2.4(1))</u>

However, these expressions lead to improved results only for continuous prismatic members. The drop panels in this example result in non-prismatic members and the following expressions should be used according to ACI 318-89:

$$I_{e,avg} = 0.50 I_e^+ + 0.25 \left(I_{e,l}^- + I_{e,r}^- \right)$$
 for interior span ACI 435R-95 (2.14)

For the middle span (span with two ends continuous) with service load level $(D+LL_{full})$:

$$I_{e,avg} = 0.50 \times 30000 + 0.25 (27503 + 27503) = 41723 \text{ in.}^4$$

$$I_{e,avg} = 0.50 I^+ + 0.50 I^-$$
 for end span ACI 435R-95 (2.14)

For the end span (span with one end continuous) with service load level $(D+LL_{full})$:

$$I_{e,avg} = 0.50 \times 26503 + 0.50 \times 22649 = 37190 \text{ in.}^4$$

Where:

 $I_{e,l}^{-}$ = The effective moment of inertia for the critical negative moment section near the left support. $I_{e,l}^{-}$ = The effective moment of inertia for the critical negative moment section near the right support. $I_{e,l}^{+}$ = The effective moment of inertia for the critical positive moment section (midspan).





Table 6 provides a summary of the required parameters and calculated values needed for deflections for exterior and interior spans.

	Table 6 – Averaged Effective Moment of Inertia Calculations												
					I	For Frame	Strip						
					M _a , kips-ft	į			I _e , in. ⁴			I _{e,avg} , in. ⁴	
Span	zone	I _g , in. ⁴	I _{cr} , in. ⁴	D	D + LL _{Sus}	D + L _{full}	M _{cr} , k-ft	D	D + LL _{Sus}	D + L _{full}	D	D + LL _{Sus}	D + L _{full}
	Left	53445	7170	-179.72	-179.72	-252.8	401.42	53445	53445	53445		37190	24576
Ext	Midspan	30000	3797	197.23	197.23	278.14	265.17	30000	30000	26503	37190		
	Right	53445	10471	-434.41	-434.41	-611.14	401.42	44379	44379	22649			
	Left	53445	10471	-388.46	-388.46	-546.48	401.42	53445	53445	27503			
Int	Mid	30000	3317	107.56	107.56	152.03	265.17	30000	30000	30000	41723	41723	28752
	Right	53445	10471	-388.46	-388.46	-546.48	401.42	53445	53445	27503			

Deflections in two-way slab systems shall be calculated taking into account size and shape of the panel, conditions of support, and nature of restraints at the panel edges. For immediate deflections in two-way slab systems, the midpanel deflection is computed as the sum of deflection at midspan of the column strip or column line in one direction (Δ_{cx} or Δ_{cy}) and deflection at midspan of the middle strip in the orthogonal direction (Δ_{mx} or Δ_{my}). Figure 21 shows the deflection computation for a rectangular panel. The average Δ for panels that have different properties in the two direction is calculated as follows:

$$\Delta = \frac{(\Delta_{cx} + \Delta_{my}) + (\Delta_{cy} + \Delta_{mx})}{2}$$

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 8)





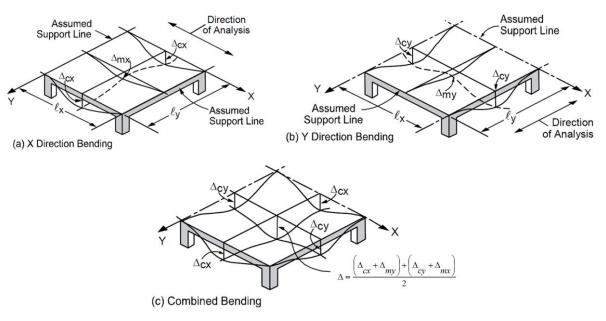


Figure 21 – Deflection Computation for a rectangular Panel

To calculate each term of the previous equation, the following procedure should be used. Figure 22 shows the procedure of calculating the term Δ_{cx} . Same procedure can be used to find the other terms.

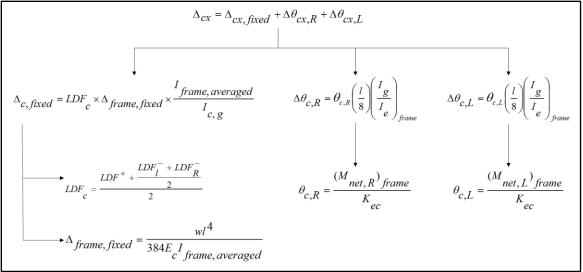


Figure $22 - \Delta_{cx}$ calculation procedure





For end span - service dead load case:

$$\Delta_{frame, fixed} = \frac{wl^4}{384E_c I_{frame, averaged}}$$

Where:

 $\Delta_{frame, fixed}$ = Deflection of column strip assuing fixed end condition.

 $w = (20 + 150 \times 10/12)(30) = 4350 \text{ lb/ft}$

$$E_c = w_c^{1.5} 33 \sqrt{f_c'} = 4287 \times 10^3 \text{ psi}$$
 ACI 318-14 (19.2.2.1.a)

 $I_{frame,averaged}$ = The averaged effective moment of inertia ($I_{e,avg}$) for the frame strip for service dead load case from Table 6 = 37190 in.⁴

$$\Delta_{frame, fixed} = \frac{(4350)(30)^4 (12)^3}{384(4287 \times 10^3)(37190)} = 0.0995 \text{ in.}$$

$$\Delta_{c,fixed} = LDF_c \times \Delta_{frame,fixed} \times \frac{I_{frame,averaged}}{I_{c,g}}$$

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 11)

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 10)

For this example and like in the spSlab program, the effective moment of inertia at midspan will be used. LDF_c is the load distribution factor for the column strip. The load distribution factor for the column strip can be found from the following equation:

$$LDF_{c} = \frac{LDF^{+} + \frac{LDF_{l}^{-} + LDF_{R}^{-}}{2}}{2}$$

And the load distribution factor for the middle strip can be found from the following equation:

$$LDF_{m} = 1 - LDF_{c}$$

For the end span, LDF for exterior negative region (LDF_L^-) , interior negative region (LDF_R^-) , and positive region (LDF_L^+) are 1.00, 0.75, and 0.60, respectively (From Table 2 of this document). Thus, the load distribution factor for the column strip for the end span is given by:



$$LDF_{c} = \frac{0.6 + \frac{1.0 + 0.75}{2}}{2} = 0.738$$

 $I_{c,g}$ = The gross moment of inertia (I_g) for the column strip for service dead load = 15000 in.⁴

$$\Delta_{c,fixed} = 0.738 \times 0.0995 \times \frac{30000}{15000} = 0.1468 \text{ in.}$$

$$\theta_{c,L} = \frac{(M_{net,L})_{frame}}{K_{ec}}$$

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 12)

Where:

 $\theta_{c,L}$ = Rotation of the span left support.

 $(M_{net,L})_{frame} = 179.72$ ft-kips = Net frame strip negative moment of the left support.

 K_{ec} = effective column stiffness = 1353×10^6 in.-lb (calculated previously).

$$\theta_{c,L} = \frac{179.72 \times 12 \times 1000}{1353 \times 10^6} = 0.00159 \text{ rad}$$

$$\Delta \theta_{c,L} = \theta_{c,L} \left(\frac{l}{8}\right) \left(\frac{I}{I_e}\right)_{frame}$$

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 14)

Where:

 $\Delta \theta_{c,L}$ = Midspan deflection due to rotation of left support.

$$\left(\frac{I_g}{I_e}\right)_{frame}$$
 = Gross-to-effective moment of inertia ratio for frame strip

$$\Delta \theta_{c,L} = 0.00159 \times \frac{30 \times 12}{8} \times \frac{30000}{37190} = 0.05786 \text{ in.}$$



$$\theta_{c,R} = \frac{(M_{net,R})_{frame}}{K_{ec}} = \frac{(611.14 - 546.48) \times 12 \times 1000}{1353 \times 10^6} = 0.00041 \text{ rad}$$

Where

 $\theta_{c,R}$ = Rotation of the end span right support.

 $(M_{net,R})_{frame}$ = Net frame strip negative moment of the right support.

$$\Delta \theta_{c,R} = \theta_{c,R} \left(\frac{l}{8} \right) \left(\frac{I_g}{I_e} \right)_{frame} = 0.00041 \times \frac{30 \times 12}{8} \times \frac{30000}{37190} = 0.01479 \text{ in.}$$

Where:

 $\Delta \theta_{c,R}$ = Midspan delfection due to rotation of right support.

$$\Delta_{cx} = \Delta_{cx, fixed} + \Delta \theta_{cx,R} + \Delta \theta_{cx,L}$$
PCA Notes on ACI 318-11 (9.5.3.4 Eq. 9)

$$\Delta_{CX} = 0.1468 + 0.01479 + 0.05786 = 0.219 \text{ in.}$$

Following the same procedure, Δ_{mx} can be calculated for the middle strip. This procedure is repeated for the equivalent frame in the orthogonal direction to obtain Δ_{cy} , and Δ_{my} for the end and middle spans for the other load levels ($D+LL_{sus}$ and $D+LL_{full}$).

Since in this example the panel is squared, $\Delta_{cx} = \Delta_{cy} = 0.219$ in. and $\Delta_{mx} = \Delta_{my} = 0.125$ in. The average Δ for the corner panel is calculated as follows:

$$\Delta = \frac{(\Delta_{cx} + \Delta_{my}) + (\Delta_{cy} + \Delta_{mx})}{2} = (\Delta_{cx} + \Delta_{my}) = (\Delta_{cy} + \Delta_{mx}) = 0.219 + 0.125 = 0.344 \text{ in.}$$



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Table 7 – Immediate (Instantaneous) Deflections in the x-direction

Col	umn	Strip
-----	-----	-------

a					D			
Span	LDF	$\Delta_{\text{frame-fixed}},$ in.	Δ _{c-fixed} , in.	θ _{c1} , rad	θ _{c2} , rad	$\Delta \theta_{c1},$ in.	$\Delta \theta_{c2},$ in.	Δ_{cx} , in.
Ext	0.738	0.0995	0.1468	0.00159	0.00041	0.05786	0.01479	0.219
Int	0.675	0.0886	0.1197	0.00041	0.00041	-0.01319	-0.01319	0.093

				D			
LDF	$\Delta_{ ext{frame-fixed}},$ in.	Δ _{m-fixed} , in.	θ _{m1} , rad	θ _{m2} , rad	$\Delta \theta_{m1},$ in.	Δθ _{m2} , in.	Δ_{mx} , in.
0.262	0.0995	0.0521	0.00159	0.00041	0.05786	0.01479	0.125
0.325	0.0886	0.0576	0.00041	0.00041	-0.01319	-0.01319	0.031

Middle Strip

G			D+LL _{sus}					
Span	LDF	$\Delta_{ ext{frame-fixed}},$ in.	$\Delta_{ ext{c-fixed}},$ in.	θ _{c1} , rad	θ _{c2} , rad	$\Delta \theta_{c1},$ in.	$\Delta \theta_{c2},$ in.	Δ_{cx} , in.
Ext	0.738	0.0995	0.1468	0.00159	0.00041	0.05786	0.01479	0.219
Int	0.675	0.0886	0.1197	0.00041	0.00041	-0.01319	-0.01319	0.093

				D+LL _{sus}			
LDF	$\Delta_{ ext{frame-fixed}},$ in.	$\Delta_{ ext{m-fixed}},$ in.	θ _{m1} , rad	θ _{m2} , rad	$\Delta \theta_{m1},$ in.	$\Delta \theta_{m2},$ in.	Δ_{mx} , in.
0.262	0.0995	0.0521	0.00159	0.00041	0.05786	0.01479	0.125
0.325	0.0886	0.0576	0.00041	0.00041	-0.01319	-0.01319	0.031

a					D+LL _{full}			
Span	LDF	$\Delta_{\text{frame-fixed}},$ in.	Δ _{c-fixed} , in.	θ _{c1} , rad	θ _{c2} , rad	$\Delta \theta_{c1},$ in.	$\Delta \theta_{c2},$ in.	$\Delta_{cx},$ in.
Ext	0.738	0.2128	0.2775	0.00224	0.00057	0.12316	0.0315	0.432
Int	0.675	0.1819	0.2455	0.00057	0.00057	-0.02693	-0.02693	0.192

				D+LL _{full}			
LDF	$\Delta_{\text{frame-fixed}},$ in.	Δ _{m-fixed} , in.	θ _{m1} , rad	θ _{m2} , rad	$\Delta \theta_{m1},$ in.	$\Delta \theta_{m2},$ in.	Δ_{mx} , in.
0.262	0.2128	0.0985	0.00224	0.00057	0.12316	0.03125	0.253
0.325	0.1819	0.1182	0.00057	0.00057	-0.02693	-0.02693	0.064

a		LL		
Span	LDF	$\Delta_{cx},$ in.		
Ext	0.738	0.213		
Int	0.675	0.098		

	LL
LDF	Δ_{mx} , in.
0.262	0.128
0.325	0.033

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5.2. Time-Dependent (Long-Term) Deflections (Δ_{lt})

The additional time-dependent (long-term) deflection resulting from creep and shrinkage (Δ_{cs}) may be estimated as follows:

$$\Delta_{cs} = \lambda_{\Delta} \times (\Delta_{sust})_{Inst}$$
PCA Notes on ACI 318-11 (9.5.2.5 Eq. 4)

The total time-dependent (long-term) deflection is calculated as:

$$(\Delta_{total})_{lt} = (\Delta_{sust})_{lnst} \times (1 + \lambda_{\Delta}) + [(\Delta_{total})_{lnst} - (\Delta_{sust})_{lnst}]$$
CSA A23.3-04 (N9.8.2.5)

Where:

 $(\Delta_{sust})_{Inst}$ = Immediate (instantaneous) deflection due to sustained load, in.

$$\lambda_{\Delta} = \frac{\xi}{1+50\rho'} \underline{ACI 318-14 (24.2.4.1.1)}$$

 $(\Delta_{total})_{lt}$ = Time-dependent (long-term) total delfection, in.

 $(\Delta_{total})_{Inst}$ = Total immediate (instantaneous) deflection, in.

For the exterior span

 ξ = 2, consider the sustained load duration to be 60 months or more. ACI 318-14 (Table 24.2.4.1.3)

 $\rho' = 0$, conservatively.

$$\lambda_{\Delta} = \frac{2}{1 + 50 \times 0} = 2$$

 $\Delta_{cs} = 2 \times 0.219 = 0.439$ in.

$$(\Delta_{total})_{lt} = 0.219 \times (1+2) + (0.432 - 0.219) = 0.871$$
 in.



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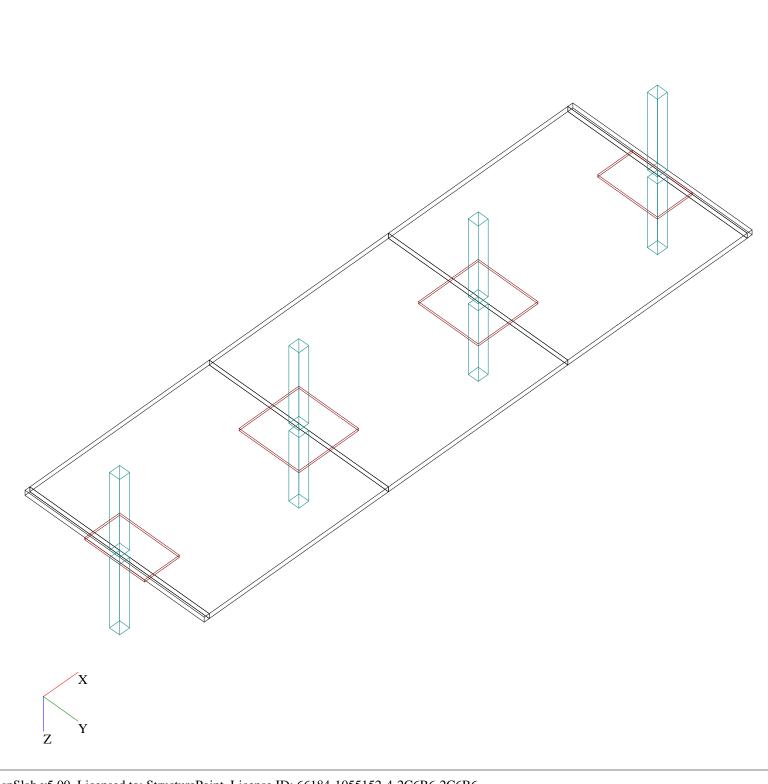
Table 8 shows long-term deflections for the exterior and interior spans for the analysis in the x-direction, for column and middle strips.

		Table 8 - Lon	g-Term Defl	ections	
		Col	umn Strip		
Span	$(\Delta_{\text{sust}})_{\text{Inst}}$, in.	λ_{Δ}	$\Delta_{\rm cs}$, in.	$(\Delta_{total})_{Inst}$, in.	$(\Delta_{ ext{total}})_{ ext{lt}}, ext{in.}$
Exterior	0.219	2.000	0.439	0.432	0.871
Interior	0.093	2.000	0.187	0.192	0.378
		Mie	ddle Strip		
Exterior	0.125	2.000	0.250	0.253	0.503
Interior	0.031	2.000	0.062	0.064	0.127

6. spSlab Software Program Model Solution

<u>spSlab</u> program utilizes the Equivalent Frame Method described and illustrated in details here for modeling, analysis and design of two-way concrete floor slab systems with drop panels. <u>spSlab</u> uses the exact geometry and boundary conditions provided as input to perform an elastic stiffness (matrix) analysis of the equivalent frame taking into account the torsional stiffness of the slabs framing into the column. It also takes into account the complications introduced by a large number of parameters such as vertical and torsional stiffness of transverse beams, the stiffening effect of drop panels, column capitals, and effective contribution of columns above and below the floor slab using the of equivalent column concept (*ACI 318-14 (R8.11.4)*).

<u>spSlab</u> Program models the equivalent frame as a design strip. The design strip is, then, separated by <u>spSlab</u> into column and middle strips. The program calculates the internal forces (Shear Force & Bending Moment), moment and shear capacity vs. demand diagrams for column and middle strips, instantaneous and long-term deflection results, and required flexural reinforcement for column and middle strips. The graphical and text results are provided below for both input and output of the <u>spSlab</u> model.



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Project: Two-Way Slab with Drop Panels

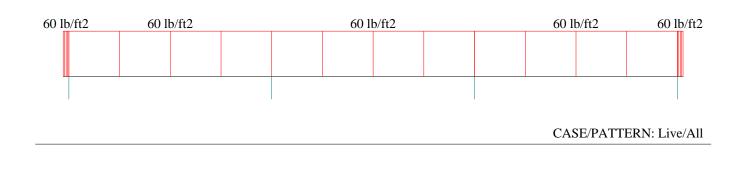
Frame: Interior Frame

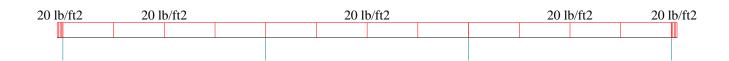
Engineer: SP

Code: ACI 318-14

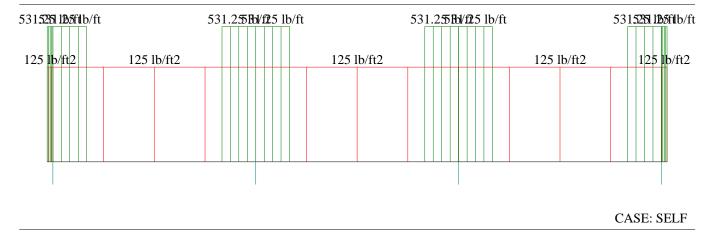
Date: 03/16/17

Time: 15:42:36





CASE: Dead



spSlab v5.00. Licensed to: StructurePoint. License ID: 66184-1055152-4-2C6B6-2C6B6

 $File: C: \ TSDA \ TSDA \ spSlab \ Two-Way \ Slab \ with \ Drop \ Panels. slb$

Project: Two-Way Slab with Drop Panels

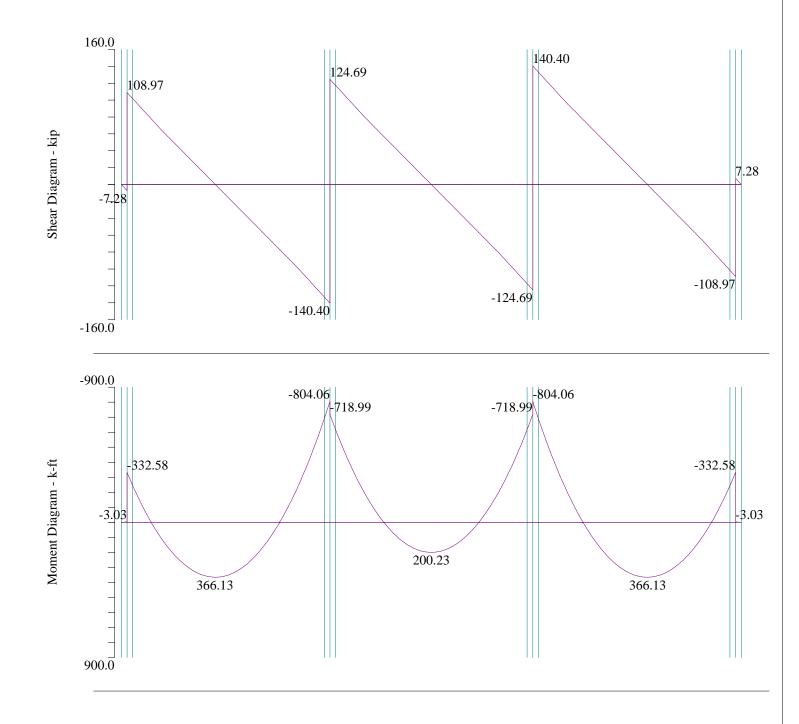
Frame: Interior Frame

Engineer: SP

Code: ACI 318-14

Date: 03/16/17

Time: 15:44:15



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Project: Two-Way Slab with Drop Panels

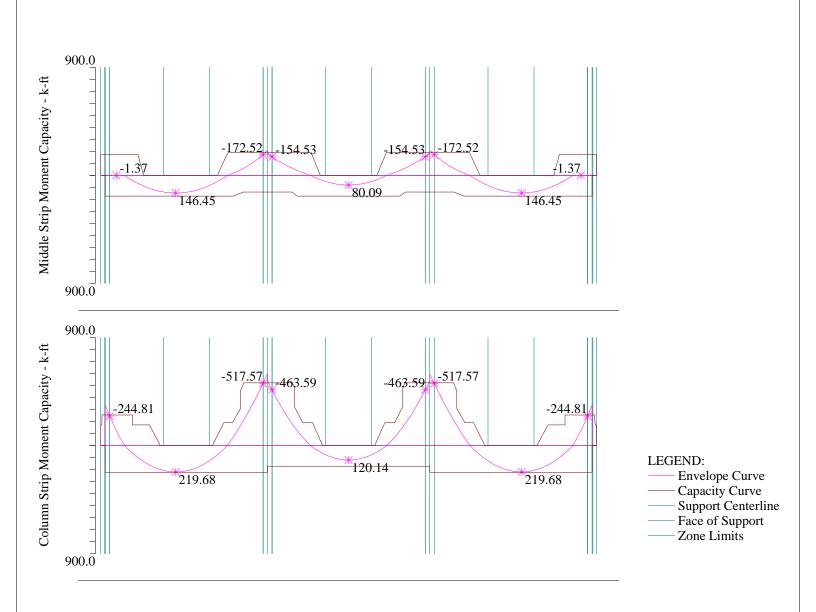
Frame: Interior Frame

Engineer: SP

Code: ACI 318-14

Date: 03/16/17

Time: 15:45:25



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Project: Two-Way Slab with Drop Panels

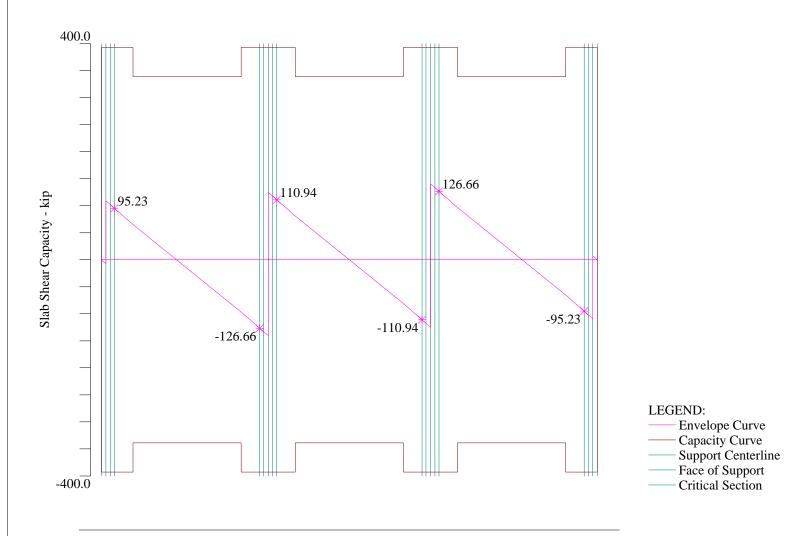
Frame: Interior Frame

Engineer: SP

Code: ACI 318-14

Date: 03/16/17

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Project: Two-Way Slab with Drop Panels

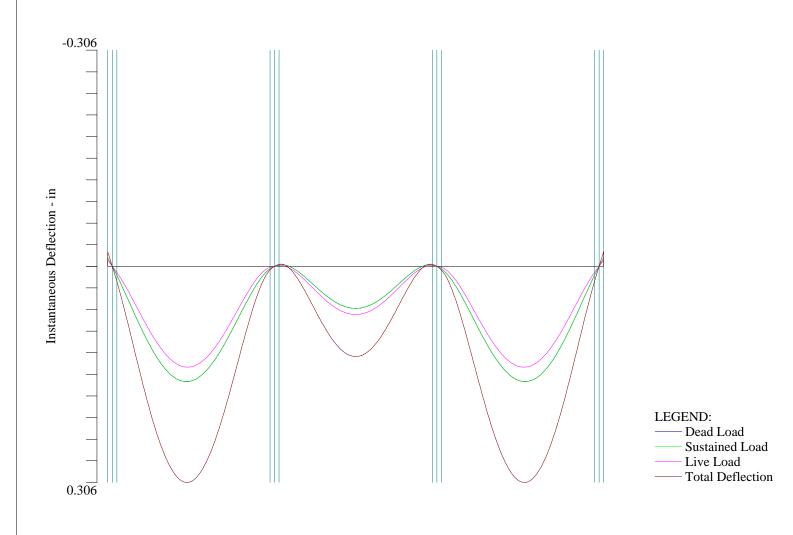
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Engineer: SP

Code: ACI 318-14

Date: 03/16/17

Time: 15:48:42



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Project: Two-Way Slab with Drop Panels

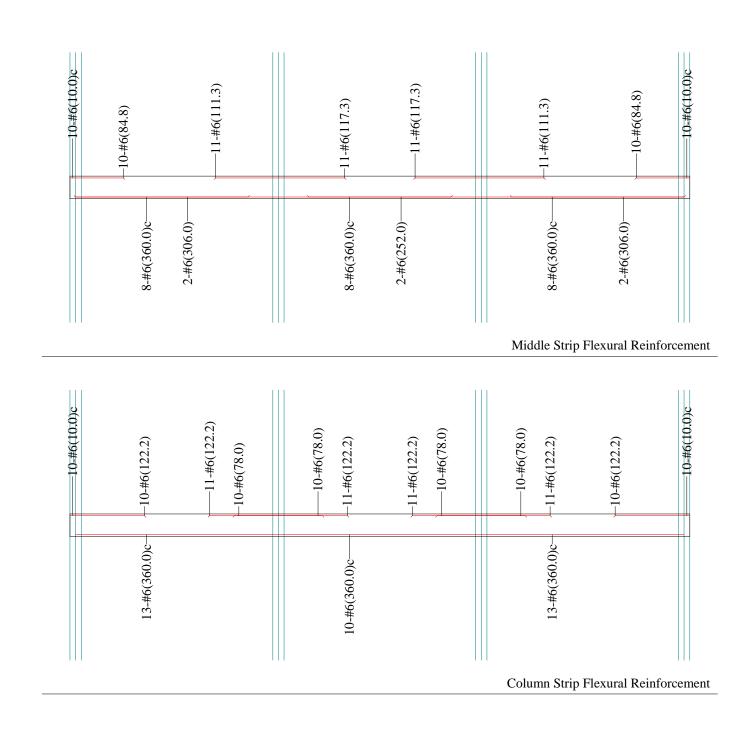
Frame: Interior Frame

Engineer: SP

Code: ACI 318-14

Date: 03/16/17

Time: 15:49:51



File: C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb

Project: Two-Way Slab with Drop Panels

Frame: Interior Frame

Engineer: SP

Code: ACI 318-14

Date: 03/16/17

Time: 15:51:11

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spSlab v5.00 (TM) A Computer Program for Analysis, Design, and Investigation of Reinforced Concrete Beams, One-way and Two-way Slab Systems Copyright © 2003-2015, STRUCTUREPOINT, LLC All rights reserved
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[1] INPUT ECHO
General Information
<pre>File name: C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb Project: Two-Way Slab with Drop Panels Frame: Interior Frame Engineer: SP Code: ACI 318-14 Reinforcement Database: ASTM A615 Mode: Design Number of supports = 4 + Left cantilever + Right cantilever Floor System: Two-Way Live load pattern ratio = 0% Minimum free edge distance for punching shear = 4 times slab thickness. Circular critical section around circular supports used (if possible). Deflections are based on cracked section properties. In negative moment regions, Ig and Mcr DO NOT include flange/slab contribution (if available) Long-term deflections are calculated for load duration of 60 months. 0% of live load is sustained. Compression reinforcement calculations NOT selected. Default incremental rebar design selected. User-defined distribution factors NOT selected. Distribution of shear to strips NOT selected. Distribution of shear to strips NOT selected. Eagen T-section design NOT selected. Longiudinal beam contribution in negative reinforcement design over support NOT selected. Transverse beam contribution in negative reinforcement design over support NOT selected.</pre>
Material Properties
Slabs/Beams Columns
wc = 150 150 lb/ft3
f'c = 5 6 ksi
Ec = 4286.8 4696 ksi fr = 0.53033 0.58095 ksi
fy = 60 ksi, Bars are not epoxy-coated fyt = 60 ksi Es = 29000 ksi
Reinforcement Database
Units: Db (in), Ab (in^2), Wb (lb/ft)

Units:	Db (in),	Ab (in^2)	, Wb (lb	/ft)			
Size	Db	Ab	Wb	Size	Db	Ab	Wb
#3	0.38	0.11	0.38	#4	0.50	0.20	0.67
#5	0.63	0.31	1.04	#6	0.75	0.44	1.50
#7	0.88	0.60	2.04	#8	1.00	0.79	2.67
#9	1.13	1.00	3.40	#10	1.27	1.27	4.30

Slab v5.00 censed to				ID: 66184	4-1055152-4	1-2C686-2	C6B6	03-16-2017, 03:5	1:55 P
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#11 #18	1.41 2.26	1.56 4.00	5.31 13.60	#14	1.69	2.25	7.65	5	
an Data	2.20	1.00	13.00						
====== Slabs									
	L. wL.	WR. L2L.	L2R (ft.);	t, Hmin (in)				
Span Loc		L1	t		wR L2	2L L	2R 	Hmin	
1 Int 2 Int	0. 30.			000 15.0 000 15.0				LC *i 10.30 *a	
3 Int 4 Int	30. 30.	000 10	0.00 15.	000 15.0 000 15.0	000 30.00	0.00	00	9.44 10.30 *a	
5 Int NOTES:				000 15.0				RC *i	
*a - Defl) is less than minimum (Hmin). r two-way construction doesn't apply due to:	
				support o					
pport Data									
Columns									
Units: cl Supp	la, c2a c1a	, clb, c2 c2a	2b (in); H Ha	a, Hb (ft) clb	c2b	Нb	Red%	3	
		20.00			20.00		100	-	
2 2	20.00 20.00	20.00 20.00	13.000 13.000	20.00 20.00	20.00 20.00	13.000 13.000	100 100		
4 2	20.00	20.00	13.000	20.00	20.00	13.000	100	0	
Drop Pane									
Supp	h	Ll	Nl, Wr (ft Lr	Wl	Wr				
1	4.25	0.833	5.000	5.000	5.000 *b				
2 3	4.25 4.25	5.000 5.000	5.000 5.000	5.000 5.000	5.000 *b 5.000 *b				
4 *b - Star	4.25 ndard d	5.000 rop.	0.833	5.000	5.000 *b				
Boundary									
		in); Kry	(kip-in/r	ad) r End A Fa	r End B				
1		 0		Fixed	Fixed				
2 3		0	0	Fixed Fixed	Fixed Fixed				
4		0	0	Fixed	Fixed				
ad Data ======									
Load Case	es and	Combinati	ons						
Case Type	SELF DEAD	Dead DEAD	Live LIVE						
	L.200	1.200	1.600						
Area Load	ls								
Units: Wa		t2)							
Case/Patt			Wa						
SELF	1 2		5.00 5.00						
	3 4	125	5.00 5.00						
Dead	5 2	125	5.00).00						
	3 4	20).00).00						
	1 5	20).00).00						
Live	2 1	60).00).00						
	3 4	60).00).00						
	5	60	0.00						
Line Load			_						
Units: Wa Case/Patt		lb/ft), I	La, Lb (ft Wa) La	Wk	D	Lb	0	

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SELF	1	531.25	-0.000	531.25	0.833
	2	531.25	0.000	531.25	5.000
	2	531.25	25.000	531.25	30.000
	3	531.25	0.000	531.25	5.000
	3	531.25	25.000	531.25	30.000
	4	531.25	0.000	531.25	5.000
	4	531.25	25.000	531.25	30.000
	5	531.25	0.000	531.25	0.833

Reinforcement Criteria

Slabs and Ribs

	Top b Min	ars Max	Bottom Min	bars Max		
Bar Size	#6	#6	#6	#6		
Bar spacing	1.00	18.00	1.00	18.00	in	
Reinf ratio	0.18	2.00	0.18	2.00	8	
Cover	0.75		0.75		in	
mbassa in NOM		10		11		10000

There is NOT more than 12 in of concrete below top bars.

Beams

	÷		Bottom b		Stirr			
	Min	Max	Min	Max		Min	Max	
Bar Size	#5	#8	#5	#8		#3	#5	
Bar spacing	1.00	18.00	1.00	18.00		6.00	18.00	in
Reinf ratio	0.14	5.00	0.14	5.00	8			
Cover	1.50		1.50		in			
Layer dist.	1.00		1.00		in			
No. of legs						2	б	
Side cover						1.50		in
lst Stirrup						3.00		in
There is NOT	more than	n 12 in c	of concrete	below	top	bars.		

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	00		00	00	00	0	00		000	0000	000	000			
	00	000	00	00		000	00		00	00	00	00			
		00	000	000		00	00		00	00	00	00			
	0	00	00		00	00	00	0	00	00	00	00			
	00	000	00		000	000	oc	0	000	0 000	00	000	(TM)		
00000 00 00000 000 00000 00000 (TM) spSlab v5.00 (TM) A Computer Program for Analysis, Design, and Investigation of Reinforced Concrete Beams, One-way and Two-way Slab Systems Copyright © 2003-2015, STRUCTUREPOINT, LLC All rights reserved															
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be responsible for either the accuracy or adequacy of the material supplied as input for processing by the spSlab computer program. Furthermore, STRUCTUREPOINT neither makes any warranty expressed nor implied with respect to the correctness of the output prepared by the spSlab program. Although STRUCTUREPOINT has endeavored to produce spSlab error free the program is not and cannot be certified infallible. The final and only responsibility for analysis, design and engineering documents is the licensee's. Accordingly, STRUCTUREPOINT disclaims all responsibility in contract, negligence or other tort for any analysis, design or engineering documents prepared in connection with the use of the spSlab program.

[2] DESIGN RESULTS*

*Unless otherwise noted, all results are in the direction of analysis only. Another analysis in the perpendicular direction has to be carried out for two-way slab systems.

Strip Widths and Distribution Factors

		_Width		Moment Factor						
Span Strip	Left**	Right**	Bottom*	Left**	Right**	Bottom*				
1 Column		15.00	15.00	1.000	1.000	0.600				
Middle		15.00	15.00	0.000	0.000	0.400				
2 Column		15.00	15.00	1.000	0.750	0.600				
Middle		15.00	15.00	0.000	0.250	0.400				
3 Column		15.00	15.00	0.750	0.750	0.600				
Middle		15.00	15.00	0.250	0.250	0.400				
4 Column		15.00	15.00	0.750	1.000	0.600				
Middle		15.00	15.00	0.250	0.000	0.400				
5 Column Middle *Used for b	15.00	15.00 15.00	15.00 15.00 **Used	1.000 0.000	0.000	0.600 0.400				

*Used for bottom reinforcement. **Used for top reinforcement.

Top Reinforcement

Units: Width (ft), Mmax (k-ft), Xmax (ft), As (ir

		Zone		Mmax	Xmax	AsMin	AsMax	AsReq	SpProv	Bars
1	Column		15.00 15.00 15.00	0.28 0.90 2.10	0.241 0.447 0.687	3.240 3.240 4.158	31.950 47.250 31.500	0.007 0.015 0.036	18.000 18.000 18.000	10-#6 *3 *5 10-#6 *3 *5 10-#6 *3
	Middle	Left Midspan Right	15.00 15.00 15.00	0.00 0.00 0.00	0.000 0.344 0.687	3.240 3.240 3.240	31.950 31.950 31.950	0.000 0.000 0.000	18.000 18.000 18.000	10-#6 *3 *5 10-#6 *3 *5 10-#6 *3 *5
2	Column	Left Midspan Right	15.00 15.00 15.00	244.81 0.00 517.57	0.833 15.000 29.167	4.158 0.000 4.158	31.500 31.950 31.500	4.225 0.000 9.137	18.000 0.000 8.571	10-#6 21-#6
	Middle	Left Midspan Right	15.00 15.00 15.00	1.37 0.00 172.52	2.059 15.000 29.167	3.240 0.000 3.240	31.950 31.950 31.950	0.034 0.000 4.406	18.000 0.000 16.364	10-#6 *3 *5 11-#6
3	Column	Left Midspan Right	15.00 15.00 15.00	463.59 0.00 463.59	0.833 15.000 29.167	4.158 0.000 4.158	31.500 31.950 31.500	8.147 0.000 8.147	8.571 0.000 8.571	21-#6 21-#6
	Middle	Left	15.00	154.53	0.833	3.240	31.950	3.938	16.364	11-#6 *5

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		Midspan	15.00	0.00	15.000	0.000	31.950	0.000	0.000	
		Right	15.00	154.53	29.167	3.240	31.950	3.938	16.364	11-#6 *5
4	Column		15.00	517.57	0.833	4.158	31.500	9.137	8.571	21-#6
		Midspan	15.00	0.00	15.000	0.000	31.950	0.000	0.000	
		Right	15.00	244.81	29.167	4.158	31.500	4.225	18.000	10-#6
	Middle	Left	15.00	172.52	0.833	3.240	31.950	4.406	16.364	11-#6
		Midspan	15.00	0.00	15.000	0.000	31.950	0.000	0.000	
		Right	15.00	1.37	27.941	3.240	31.950	0.034	18.000	10-#6 *3 *5
5	Column	Left	15.00	2.10	0.146	4.158	31.500	0.036	18.000	10-#6 *3
		Midspan	15.00	0.90	0.386	3.240	47.250	0.015	18.000	10-#6 *3 *5
		Right	15.00	0.28	0.593	3.240	31.950	0.007	18.000	10-#6 *3 *5
	Middle	Left	15.00	0.00	0.146	3.240	31.950	0.000	18.000	10-#6 *3 *5
		Midspan	15.00	0.00	0.490	3.240	31.950	0.000	18.000	10-#6 *3 *5
		Right	15.00	0.00	0.833	3.240	31.950	0.000	18.000	10-#6 *3 *5
	~		==,	2.00			2 =			=

NOTES:

*3 - Design governed by minimum reinforcement.*5 - Number of bars governed by maximum allowable spacing.

Top Bar Details

Units: Length (ft)

	. ,	Left	t		Conti	nuous		Rig	ht	
Span Strip	Bars	Length								
1 Column					10-#6	0.83				
Middle					10-#6	0.83				
2 Column	10-#6	10.18					11-#6	10.18	10-#6	6.50
Middle	10-#6	7.07					11-#6	9.27		
3 Column	11-#6	10.18	10-#6	6.50			11-#6	10.18	10-#6	6.50
Middle	11-#6	9.77					11-#6	9.77		
4 Column	11-#6	10.18	10-#6	6.50			10-#6	10.18		
Middle	11-#6	9.27					10-#6	7.07		
5 Column					10-#6	0.83				
Middle					10-#6	0.83				

Top Bar Development Lengths

------Units: Length (in)

		Le	ft		Conti	.nuous		Rig	ht	
Span Stri	.p Bar	s DevLen	Bars	DevLen	Bars	DevLen	Bars	DevLen	Bars	DevLen
1 Colu	ımn – –	_			10-#6	12.00				
Midd	lle	-			10-#6	12.00				
2 Colu	umn 10-‡	6 24.44					11-#6	25.17	10-#6	25.17
Midd							11-#6	23.17		
3 Colu	ımn 11-‡	6 22.44	10-#6	22.44			11-#6	22.44	10-#6	22.44
Midd				22.11			11-#6	22.44	10-#0	22.44
4 Colu	ımn 11-‡	6 25.17	10-#6	25.17			10-#6	24.44		
Midd	lle 11-‡	6 23.17					10-#6	12.00		
5 Colu		_			10-#6	12.00				
Midd		-			10-#6	12.00				

Bottom Reinforcement

Units: Width Span Strip	(ft), Mmax Width	(k-ft), Z Mmax	Xmax (ft), Xmax	As (in^2 AsMin	2), Sp (in AsMax) AsReq	SpProv	Bars
1 Column Middle	15.00 15.00	0.00 0.00	0.344 0.344	0.000 0.000	31.950 31.950	0.000	0.000 0.000	
2 Column	15.00	219.68	13.000	3.240	31.950	5.641	13.846	13-#6
Middle	15.00	146.45	13.000	3.240	31.950	3.728	18.000	10-#6 *5
3 Column	15.00	120.14	15.000	3.240	31.950	3.049	18.000	10-#6 *3 *5
Middle	15.00	80.09	15.000	3.240	31.950	2.024	18.000	10-#6 *3 *5
4 Column	15.00	219.68	17.000	3.240	31.950	5.641	13.846	13-#6
Middle	15.00	146.45	17.000	3.240	31.950	3.728	18.000	10-#6 *5
5 Column Middle NOTES:	15.00 15.00	0.00 0.00	0.490 0.490	0.000 0.000	31.950 31.950	0.000 0.000	0.000 0.000	

*3 - Design governed by minimum reinforcement.
*5 - Number of bars governed by maximum allowable spacing.

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Bottom Bar Details

Units: Start (ft), Length (ft)

0111 01	Deare		ng Bars		Short Bars				
			5						
Span	Strip	Bars	Start	Length	Bars	Start	Length		
1	a . 1								
T	Column								
	Middle								
~	a 1	10 110	0 00	20.00					
2		13-#6		30.00					
	Middle	8-#6	0.00	30.00	2-#6	0.00	25.50		
2	a 1	10 110	0 0 0	20.00					
3	Column	10-#6	0.00	30.00					
	Middle	8-#6	0.00	30.00	2-#6	4.50	21.00		
4	Column	13-#6	0.00	30.00					
	Middle	8-#6	0.00	30.00	2-#6	4.50	25.50		
		0 11 0	0.00	50.00	2 11 0	1.00	20.00		
	_								
5	Column								
	Middle								

Bottom Bar Development Lengths

Units: DevLen (in)

0112.01	<i>DO1</i>	(===)			
		Long	Bars	Short	Bars
Span	Strip	Bars	DevLen	Bars	DevLen
1	Column				
	Middle				
2	Column	13-#6	25.10		
	Middle	8-#6	21.57	2-#6	21.57
3	Column	10-#6	17.64		
	Middle	8-#6	12.00	2-#6	12.00
4	Column	13-#6	25.10		
	Middle	8-#6	21.57	2-#6	21.57
5	Column				
	Middle				

Flexural Capacity

Units: x (ft), As (in^2), PhiMn, Mu (k-ft)

			-1.1	Тој					-1.1	Bottor			
n Strip	х	AsTop	PhiMn-	Mu	Comb	Pat	Status	AsBot	PhiMn+	Mu+	Comb	Pat	Status
1 Column	0.000	4.40	-172.31	0.00	U1	A11	OK	0.00	0.00	0.00	U1	A11	OK
	0.241	4.40	-256.46	-0.28	U1	All	OK	0.00	0.00	0.00	U1	All	OK
	0.417	4.40	-256.46	-0.76	U1	All	OK	0.00	0.00	0.00	U1	All	OK
	0.447	4.40	-254.75	-0.90	U1	All	OK	0.00	0.00	0.00	U1	All	OK
	0.687	4.40	-254.75	-2.10	U1	All	OK	0.00	0.00	0.00	U1	All	OK
	0.833	4.40	-254.75	-3.03	U1	A11		0.00	0.00	0.00	U1	All	
Middle	0.000	4.40	-172.31	0.00	U1	A11	OK	0.00	0.00	0.00	U1	All	OK
	0.241	4.40	-172.31	-0.00	U1	All	OK	0.00	0.00	0.00	U1	All	OK
	0.417	4.40	-172.31	-0.00	U1	All	OK	0.00	0.00	0.00	U1	All	OK
	0.447	4.40	-172.31	-0.00	U1	All	OK	0.00	0.00	0.00	U1	All	OK
	0.687	4.40	-172.31	-0.00	U1	All	OK	0.00	0.00	0.00	U1	All	OK
	0.833	4.40	-172.31	-0.00	U1	All		0.00	0.00	0.00	U1	All	
2 Column	0.000	4.40	-254.75	-335.03	U1	All		5.72	222.67	0.00	U1	All	
	0.625	4.40	-254.75	-266.67	U1	A11		5.72	222.67	0.00	U1	All	
	0.833	4.40	-254.75	-244.81	U1	A11	OK	5.72	222.67	0.00	U1	All	OK
	5.000	4.40	-254.75	0.00	U1	All	OK	5.72	222.67	61.82	U1	All	OK
	5.000	4.40	-172.31	0.00	U1	All	OK	5.72	222.67	61.84	U1	All	OK
	8.146	4.40	-172.31	0.00	U1	All	OK	5.72	222.67	160.99	U1	All	OK
	10.183	0.00	0.00	0.00	U1	All	OK	5.72	222.67	199.55	U1	All	OK
	10.750	0.00	0.00	0.00	U1	All	OK	5.72	222.67	206.72	U1	All	OK
	13.000	0.00	0.00	0.00	U1	All	OK	5.72	222.67	219.68	U1	All	OK
	15.000	0.00	0.00	0.00	U1	All	OK	5.72	222.67	210.54	U1	All	OK
	19.250	0.00	0.00	0.00	U1	All	OK	5.72	222.67	126.57	U1	All	OK
	19.817	0.00	0.00	0.00	U1	All	OK	5.72	222.67	108.71	U1	All	OK
	21.914	4.84	-189.16	0.00	U1	A11	OK	5.72	222.67	29.13	U1	All	OK
	23.500	4.84	-189.16	-60.24	U1	A11	OK	5.72	222.67	0.00	U1	All	OK
	25.000	7.99	-307.67	-166.19	U1	All	OK	5.72	222.67	0.00	U1	All	OK
	25.000	7.99	-454.84	-166.23	U1	A11	OK	5.72	222.67	0.00	U1	All	OK
	25.598	9.24	-523.14	-211.55	U1	All	OK	5.72	222.67	0.00	U1	All	OK
	29.167	9.24	-523.14	-517.57	U1	All	OK	5.72	222.67	0.00	U1	All	OK
	29.375	9.24	-523.14	-537.19	U1	A11		5.72	222.67	0.00	U1	All	
	30.000	9.24	-523.14	-597.13	U1	All		5.72	222.67	0.00	U1	All	
Middle	0.000	4.40	-172.31	2.45		A11		4.40	172.31	0.00		All	
	0.833	4.40	-172.31	-0.00		A11	OK	4.40	172.31	0.00		All	OK
	2.059	4.40	-172.31	-1.37		A11	OK	4.40	172.31	0.00		All	OK
	6.067	4.40	-172.31	0.00		A11	OK	4.40	172.31	67.21		All	OK
	7.067	0.00	0.00	0.00		A11	OK	4.40	172.31	88.25		A11	OK
	10.750	0.00	0.00	0.00		A11	OK	4.40	172.31	137.81		All	OK

C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb 0.00 172.31 146.45 U1 All OK 13.000 0.00 0.00 U1 All OK 4.40 15.000 0.00 0.00 0.00 U1 All OK 4.40 172.31 140.36 U1 All 0.00 19.250 0.00 0.00 U1 All OK 4.40 172.31 84.38 U1 All 0.00 20.729 0.00 0.00 U1 All OK 4.40 172.31 51.16 U1 All 0.00 -189.16 -1.38 22.660 4.84 U1 All OK 4.40 172.31 U1 All 23.702 4.84 -189.16 -18.69 U1 All OK 4.40 172.31 0.00 Ul All -189.16 -56.75 25.500 4.84 U1 All OK 3.52 138.39 0.00 U1 All -189.16 -172.52 29.167 4.84 U1 All OK 3.52 138.39 0.00 U1 All 0.00 29.583 4.84 -189.16 -189.32 U1 All ___ 3.52 138.39 U1 All 30.000 4.84 -189.16 -206.93 Ul All ____ 3.52 138.39 0.00 U1 All 3 Column 0.000 9.24 -523.14 -539.24 Ul All 4.40 172.31 0.00 Ul All _ _ _ 0.833 9.24 -523.14-463.59 Ul All OK 4.40 172.31 0.00 Ul All 4.630 9.24 -523.14 -176.57 U1 All OK 4.40 172.31 0.00 U1 All -475.78 4.40 5.000 8.37 -153.60 U1 All OK 172.31 0.00 Ul All -321.84 -153.56 172.31 0.00 5.000 8.37 U1 All OK 4.40 U1 All -189.16 -69.29 OK 4.40 172.31 0.00 U1 All 6.500 4.84 U1 All 8.313 4.84 -189.16 0.00 U1 All OK 4.40 172.31 11.45 U1 All 0.00 10.183 0.00 Ul All 4.40 172.31 63.73 0.00 OK Ul All 0.00 172.31 76.24 10.750 0.00 0.00 U1 All OK 4.40 U1 All 15.000 0.00 0.00 4.40 172.31 0.00 U1 All OK 120.14 U1 All 19.250 0.00 0.00 0.00 U1 All OK 4.40 172.31 76.24 U1 All 0.00 0.00 4.40 172.31 19.817 0.00 U1 All OK 63.73 Ul All 21.687 4.84 -189.16 0.00 U1 All OK 4.40 172.31 11.45 U1 All -189.16 172.31 0.00 -69.29 4.40 23.500 4.84 U1 All OK U1 All 25.000 8.37 -321.84 -153.56 U1 All OK 4.40 172.31 0.00 Ul All 172.31 25.000 8.37 -475.78 -153.60 U1 All OK 4.40 0.00 U1 All 25.370 9.24 -523.14 -176.57 U1 All OK 4.40 172.31 0.00 U1 All -523.14 -463.59 Ul All OK 172.31 Ul All 29.167 9.24 4.40 0.00 30.000 9.24 -523.14 -539.24 U1 All ---4.40 172.31 0.00 Ul All Middle 0.000 4.84 -189.16 -179.75 U1 All ____ 3.52 138.39 0.00 Ul All -189.16 OK 3.52 0.00 4.84 -154.53U1 All 138.39 U1 All 0.833 3.52 0.00 -189.16 OK 4.500 4.84 -61.59 U1 All 138.39 U1 All 5.500 4.84 -189.16 -41.32 U1 All OK 4.40 172.31 0.00 U1 All 172.31 8.045 4.84 -189.16 0.00 U1 All OK 4.40 1.71 U1 All 0.00 0.00 0.00 OK 4.40 172.31 35.79 9.771 U1 All U1 All 10.750 0.00 0.00 0.00 U1 All OK 4.40 172.31 50.83 U1 All 15.000 0.00 0.00 0.00 U1 All OK 4.40 172.31 80.09 U1 All 172.31 0.00 4.40 19.250 0.00 0.00 U1 All OK 50.83 Ul All 172.31 35.79 20.229 0.00 0.00 0.00 U1 All OK 4.40 U1 All 4.84 -189.16 0.00 1.71 21.955 U1 All OK 4.40 172.31 U1 All 24.500 4.84 -189.16 -41.32 Ul All OK 4.40 172.31 0.00 U1 All 25.500 4.84 -189.16 -61.59 U1 All OK 3.52 138.39 0.00 U1 All 29.167 4.84 -189.16 -154.53 U1 All OK 3.52 138.39 0.00 U1 All -189.16 -179.75 30.000 4.84 U1 All ____ 3.52 138.39 0.00 U1 All 4 Column 0.000 9.24 -523.14 -597.13 Ul All ____ 5.72 222.67 0.00 Ul All -537.19 0.625 9.24 -523.14 U1 All _ _ _ 5.72 222.67 0.00 U1 All 0.00 -523.14 -517.57 Ul All OK 5.72 Ul All 0.833 9.24 222.67 4.402 9.24 -523.14 -211.55 U1 All OK 5.72 222.67 0.00 U1 All 5.000 7.99 -454.84 -166.23 U1 All OK 5.72 222.67 0.00 U1 All -307.67 0.00 5.000 7.99 -166.19 U1 All OK 5.72 222.67 U1 All -189.16 OK 5.72 222.67 0.00 6.500 4.84 -60.24 U1 All U1 All 8.086 4.84 -189.16 0.00 U1 All OK 5.72 222.67 29.13 U1 All 10.183 0.00 0.00 0.00 U1 All OK 5.72 222.67 108.71 Ul All 0.00 5.72 U1 All 10.750 0.00 0.00 U1 All OK 222.67 126.57 0.00 0.00 210.54 0.00 5.72 222.67 15.000 U1 All OK U1 All 17.000 0.00 0.00 0.00 Ul All OK 5.72 222.67 219.68 U1 All 19.250 0.00 0.00 0.00 Ul All OK 5.72 222.67 206.72 U1 All 0.00 0.00 199.55 19.817 0.00 U1 All OK 5.72 222.67 U1 All -172.31 160.99 21.854 4.40 0.00 U1 All OK 5.72 222.67 U1 All 25.000 4.40 -172.31 0.00 U1 All OK 5.72 222.67 61.84 Ul All 25.000 4.40 -254.75 0.00 Ul All OK 5.72 222.67 61.82 Ul All -254.75 -244.81 5.72 222.67 0.00 29.167 4.40 U1 All OK U1 All 0.00 29.375 4.40 -254.75 -266.68 U1 All ___ 5.72 222.67 U1 All 30.000 4.40 -254.75 -335.03 U1 All _ _ _ 5.72 222.67 0.00 U1 All ____ Middle 0.000 4.84 -189.16 -206.93 Ul All 3.52 138.39 0.00 U1 All 0.00 0.417 4.84 -189.16 -189.32_ _ _ U1 All 3.52 138.39 U1 All 4.84 -189.16 -172.52OK 3.52 138.39 0.00 0.833 U1 All U1 All 4.500 4.84 -189.16 -56.75 U1 All OK 3.52 138.39 0.00 Ul All 172.31 -189.16 -18.69 4.40 U1 All 6.298 4.84 U1 All OK 0.00 7.340 4.84 -189.16 -1.38 U1 All OK 4.40 172.31 0.00 U1 All 9.271 0.00 0.00 4.40 172.31 51.16 OK 0.00 U1 All U1 All 10.750 0.00 0.00 0.00 Ul All OK 4.40 172.31 84.38 Ul All 172.31 15.000 0.00 0.00 0.00 U1 All OK 4.40 140.36 U1 All 17.000 0.00 0.00 0.00 U1 All OK 4.40 172.31 146.45 U1 All 19.250 0.00 0.00 0.00 U1 All OK 4.40 172.31 137.81 U1 All 22.933 0.00 0.00 0.00 Ul All OK 4.40 172.31 88.25 U1 All 23,933 4.40 -172.31 0.00 Ul All OK 4.40 172.31 67.21 Ul All -172.31 -1.37 U1 All 172.31 0.00 U1 All 27.941 4.40 OK 4.40 OK 4.40 4.40 -172.31 -0.00 U1 All 172.31 0.00 Ul All 29.167 30.000 4.40 -172.31 2.45 Ul All ___ 4.40 172.31 0.00 U1 All -3.03 0.00 5 Column 0.000 4.40 -254.75U1 All 0.00 0.00 U1 All _ _ _

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-256.46

-256.46

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C. (ISDA (ISDA-Sp	SIAD-IWC	o-way S.	Tab with Dro	op Paneis	.SID						
	0.593	4.40	-172.31	-0.28	U1 All	OK	0.00	0.00	0.00	U1 All	OK
	0.833	4.40	-172.31	-0.00	U1 All	OK	0.00	0.00	0.00	U1 All	OK
Middle	0.000	4.40	-172.31	-0.00	U1 All		0.00	0.00	0.00	U1 All	
	0.146	4.40	-172.31	-0.00	U1 All	OK	0.00	0.00	0.00	U1 All	OK
	0.386	4.40	-172.31	-0.00	U1 All	OK	0.00	0.00	0.00	U1 All	OK
	0.417	4.40	-172.31	-0.00	U1 All	OK	0.00	0.00	0.00	U1 All	OK
	0.593	4.40	-172.31	-0.00	U1 All	OK	0.00	0.00	0.00	U1 All	OK
	0.833	4.40	-172.31	-0.00	Ul All	OK	0.00	0.00	0.00	Ul All	OK
Slab Shear Capa	city										
Units: b, d	(in) X1	(f+)	PhiVc Vu()	kin)							
	b	. , ,	ratio	PhiVc		Vu	Xu				

Span	b	d	Vratio	PhiVc	Vu	Xu
1	360.00	8.88	1.000	338.88	7.28	-0.00
	360.00	10.29	1.000	392.97	7.28	-0.00
2	360.00	10.29	1.000	392.97	95.23	1.57
	360.00	8.88	1.000	338.88	96.72	25.00
	360.00	10.29	1.000	392.97	126.66	28.43
3	360.00	10.29	1.000	392.97	110.94	1.57
	360.00	8.88	1.000	338.88	81.00	25.00
	360.00	10.29	1.000	392.97	110.94	28.43
4	360.00	10.29	1.000	392.97	126.66	1.57
	360.00	8.88	1.000	338.88	96.72	5.00
	360.00	10.29	1.000	392.97	95.23	28.43
5	360.00	10.29	1.000	392.97	0.00	0.83
	360.00	8.88	1.000	338.88	0.00	0.83

Flexural Transfer of Negative Unbalanced Moment at Supports

Units:	Width	(in).	Munb	(k-ft.).	As	(in^2)

Supp	Width	Width-c	d	Munb	Comb	Pat	GammaF	AsReq	AsProv A	Add Bars
1	62.75	62.75	13.13	329.55	U1	All	0.626	3.605	1.534	5-#6
2	62.75	62.75	13.13	85.07	U1	All	0.600	0.871	3.221	
3	62.75	62.75	13.13	85.07	U1	All	0.600	0.871	3.221	
4	62.75	62.75	13.13	329.55	U1	All	0.626	3.605	1.534	5-#6

Punching Shear Around Columns

Critical Section Properties ------

Units: bl, Supp Type	b2, b0, b1	5, ,	c(left), b0	c(right) davg	. , ,	. , ,	Jc (in^4) c(right)	Ac	Jc
1 Rect	26.56	33.13	86.25	13.13	8.38	18.38	8.18	1132	98239
2 Rect	33.13	33.13	132.50	13.13	0.00	16.56	16.56	1739.1	3.3052e+005
3 Rect	33.13	33.13	132.50	13.13	0.00	16.56	16.56	1739.1	3.3052e+005
4 Rect	26.56	33.13	86.25	13.13	-8.38	8.18	18.38	1132	98239

Punching Shear Results _____

Units:	Vu (kip), Munb) (k-ft), v	u (psi),	Phi*v	/c (pa	si)		
Supp	Vu	vu	Munb	Comb	Pat	GammaV	vu	Phi*vc
1	114.58	101.2	249.52	U1	All	0.374	194.4	212.1
2	262.99	151.2	-85.07	U1	All	0.400	171.7	212.1
3	262.99	151.2	85.07	U1	All	0.400	171.7	212.1
4	114.58	101.2	-249.52	U1	All	0.374	194.4	212.1

Punching Shear Around Drops

Critical Section Properties ------

Units: bl,	b2, b0,	davg, CG,	c(left),	c(right)	(in), Ac	(in^2),	Jc (in^4)		
Supp Type	b1	b2	b0	davg	CG	c(left)	c(right)	Ac	Jc
1 Rect	74.44	128.88	277.75	8.88	44.49	54.49	19.95	2465	1.468e+006
2 Rect	128.88	128.88	515.50	8.88	0.00	64.44	64.44	4575.1	1.2679e+007
3 Rect	128.88	128.88	515.50	8.88	0.00	64.44	64.44	4575.1	1.2679e+007
4 Rect	74.44	128.88	277.75	8.88	-44.49	19.95	54.49	2465	1.468e+006

Punching Shear Results _____

					i) Phi*vc
98.24	U1	All	39	.9	156.9
233.91	U1	All	51	.1	142.6
233.91	U1	All	51	.1	142.6
98.24	U1	All	39	.9	156.9
	Vu 98.24 233.91 233.91		Vu Comb Pat 98.24 U1 All 233.91 U1 All 233.91 U1 All	Vu Comb Pat 98.24 U1 All 39 233.91 U1 All 51 233.91 U1 All 51	98.24 U1 All 39.9 233.91 U1 All 51.1 233.91 U1 All 51.1

Material Takeoff

Reinforcement in the Direction of Analysis _____ _____

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Bottom Bars:2919.9 lb<=>31.85 lb/ft<=>1.062 lb/ft^2Stirrups:0.0 lb<=>0.00 lb/ft<=>0.000 lb/ftTotal Steel:5180.9 lb<=>56.52 lb/ft<=>1.884 lb/ft^2Concrete:2403.8 ft^3 <=>26.22 ft^3/ft<=>0.874 ft^3/ft^2

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program is not and analysis, design STRUCTUREPOINT dis	cannot and claims al	be eng 1 re	certi ineer: spons:	fied ing ibilit	infal docum y in	lible. ents contra	The is ct, ne	inal a the gligen	nd li .ce o	only cens r ot	pSlab error free the responsibility for ee's. Accordingly, her tort for any use of the spSlab
[3] DEFLECTION RESULTS		=====	=====		=====		=====				
Section Properties											

Frame Section Properties

Units: Ig, Icr (in⁴), Mcr (k-ft)

			M+ve		M-ve				
Span	Zone	Ig	Icr	Mcr	Ig	Icr	Mcr		
1	Left	30000	0	265.17	30000	3641	-265.17		
	Midspan	30000	0	265.17	30000	3641	-265.17		
	Right	53445	0	282.33	53445	7174	-401.42		
2	Left	53445	3164	282.33	53445	7174	-401.42		
	Midspan	30000	3800	265.17	30000	0	-265.17		
	Right	53445	3164	282.33	53445	10477	-401.42		
3	Left	53445	2799	282.33	53445	10477	-401.42		
	Midspan	30000	3319	265.17	30000	0	-265.17		
	Right	53445	2799	282.33	53445	10477	-401.42		
4	Left	53445	3164	282.33	53445	10477	-401.42		
	Midspan	30000	3800	265.17	30000	0	-265.17		
	Right	53445	3164	282.33	53445	7174	-401.42		
5	Left	53445	0	282.33	53445	7174	-401.42		
	Midspan	30000	0	265.17	30000	3641	-265.17		
	Right	30000	0	265.17	30000	3641	-265.17		

NOTES: M+ve values are for positive moments (tension at bottom face). M-ve values are for negative moments (tension at top face).

Frame Effective Section Properties

Units: Ie, Ie, avg (in^4), Mmax (k-ft)

OILTC	3· 10, 10,	avg (III I), muar (it	IC/							
			Load Level								
			De	ead	Sust	ained	Dead	+Live			
Span	Zone	Weight	Mmax	Ie	Mmax	Ie	Mmax	Ie			
1	Right	1.000	-1.69	53445	-1.69	53445	-2.32	53445			
	Span Avg			53445		53445		53445			
2	Middle	0.500	197.23	30000	197.23	30000	278.14	26502			
	Right	0.500	-434.41	44379	-434.41	44379	-611.14	22653			
	Span Avg			37189		37189		24578			
3	Left	0.250	-388.46	53445	-388.46	53445	-546.48	27506			
	Middle	0.500	107.56	30000	107.56	30000	152.03	30000			
	Right	0.250	-388.46	53445	-388.46	53445	-546.48	27506			
	Span Avg			41723		41723		28753			
4	Left	0.500	-434.41	44379	-434.41	44379	-611.14	22653			
	Middle	0.500	197.23	30000	197.23	30000	278.14	26502			
	Span Avg			37189		37189		24578			
5	Left	1.000	-1.69	53445	-1.69	53445	-2.32	53445			
	Span Avg			53445		53445		53445			

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Units:	Ig	(in^4)	

	, ,		Ratio	Middle Ig		Ratio
1 2 3 4 5	15000 15000 15000	0.800 0.738 0.675 0.738 0.800	1.475 1.350 1.475	15000 15000 15000	0.200 0.262 0.325 0.262 0.262 0.200	0.525 0.650 0.525

NOTES: Load distirubtion factor, LDL, averages moment distribution factors listed in [2] Design Results. Ratio refers to proportion of strip to frame deflections under fix-end condtions.

Instantaneous Deflections

Extreme Instantaneous Frame Deflections and Corresponding Locations

Units:	Def	(in),	Loc	(ft)
0112.00	201	(/ /	200	(20)

		(,, (,		Live		Total		
pan Directio	on Valu	rection Value Dead	Sustained Un	sustained	Total	Sustained	Dead+Live	
1 Dor	wn De	Down Def						
	Lo	Loc						
T	Up De	Up Def -0.012		-0.008	-0.008	-0.012	-0.021	
	- Lo	Loc 0.000		0.000	0.000	0.000	0.000	
2 Dov	wn De	Down Def 0.163		0.143	0.143	0.163	0.306	
	Lo	Loc 13.750		14.000	14.000	13.750	13.750	
T	Up De	Up Def						
	- Lo	Loc						
3 Dot	wn De	Down Def 0.060		0.068	0.068	0.060	0.128	
	Lo	Loc 15.000		15.000	15.000	15.000	15.000	
T	Up De	Up Def -0.002		-0.001	-0.001	-0.002	-0.003	
	- Lo	Loc 1.324		1.078	1.078	1.324	1.078	
4 Dou	wn De	Down Def 0.163		0.143	0.143	0.163	0.306	
	Lo	Loc 16.250		16.000	16.000	16.250	16.250	
T	Up De	Up Def						
	- Lo	Loc						
5 Dot	wn De	Down Def						
	Lo	Loc						
T	Up De	Up Def -0.012		-0.008	-0.008	-0.012	-0.021	
	-	Loc 0.833		0.833	0.833	0.833	0.833	
τ	-	-						

Extreme Instantaneous Column Strip Deflections and Corresponding Locations

Units: Def (in), Loc (ft)

0					Live	Total		
Span Di	rection `	Value	Dead	Sustained	Unsustained	Total	Sustained	Dead+Live
1	Down	Def						
		Loc						
	Up	Def	-0.012		-0.008	-0.008	-0.012	-0.021
	-	Loc	0.000		0.000	0.000	0.000	0.000
2	Down	Def	0.207		0.188	0.188	0.207	0.395
		Loc	14.000		14.250	14.250	14.000	14.000
	Up	Def						
	_	Loc						
3	Down	Def	0.089		0.096	0.096	0.089	0.185
		Loc	15.000		15.000	15.000	15.000	15.000
	Up	Def	-0.002		-0.001	-0.001	-0.002	-0.002
	-	Loc	1.078		0.833	0.833	1.078	1.078
4	Down	Def	0.207		0.188	0.188	0.207	0.395
		Loc	16.000		15.750	15.750	16.000	16.000
	Up	Def						
	_	Loc						
5	Down	Def						
		Loc						
	Up	Def	-0.012		-0.008	-0.008	-0.012	-0.021
	-	Loc	0.833		0.833	0.833	0.833	0.833

Extreme Instantaneous Middle Strip Deflections and Corresponding Locations

Units: Def (in), Loc (ft)

011100	Der (III	// 100 (Live		Tota	al
Span Direction Value		Dead	Sustained Unsustained		Total	Sustained	Dead+Live	
1	Down	Def				·		
		Loc						
	Up	Def	-0.012		-0.008	-0.008	-0.012	-0.021
		Loc	0.000		0.000	0.000	0.000	0.000
2	Down	Def	0.120		0.098	0.098	0.120	0.218
		Loc	13.000		13.250	13.250	13.000	13.250
	Up	Def						
		Loc						
3	Down	Def	0.030		0.040	0.040	0.030	0.071
		Loc	15.000		15.000	15.000	15.000	15.000
	Up	Def	-0.003		-0.001	-0.001	-0.003	-0.004
		Loc	1.814		1.324	1.324	1.814	1.569

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4	Down	Def	0.120	 0.098	0.098	0.120	0.218
		Loc	17.000	 16.750	16.750	17.000	16.750
	Up	Def		 			
		Loc		 			
5	Down	Def		 			
		Loc		 			
	Up	Def	-0.012	 -0.008	-0.008	-0.012	-0.021
		Loc	0.833	0.833	0.833	0.833	0.833

Long-term Deflections

Long-term Column Strip Deflection Factors

Time dependant factor for sustained loads = 2.000

Units: Astop, Asbot (in^2), b, d (in), Rho' (%), Lambda (-)

			M+\	/e				M	I-ve		
Span	Zone	Astop	b	d	Rho '	Lambda	Asbot	b	d	Rho '	Lambda
1	Right				0.000	2.000				0.000	2.000
2	Midspan				0.000	2.000				0.000	2.000
3	Midspan				0.000	2.000				0.000	2.000
4	Midspan				0.000	2.000				0.000	2.000
5	Left				0.000	2.000				0.000	2.000

NOTES: Deflection multiplier, Lambda, depends on moment sign at sustained load level and Rho' in given zone. Rho' is assumed zero because Compression Reinforcement option is NOT selected in Solve Options.

Long-term Middle Strip Deflection Factors

Time dependant factor for sustained loads = 2.000 Units: Astop, Asbot (in^2), b, d (in), Rho' (%), Lambda (-)

	_		M	+ve	veM-ve							
Span	Zone	Astop	b	d	Rho '	Lambda	Asbot	b	d	Rho'	Lambda	
1	Right				0.000	2.000				0.000	2.000	
2	Midspan				0.000	2.000				0.000	2.000	
3	Midspan				0.000	2.000				0.000	2.000	
4	Midspan				0.000	2.000				0.000	2.000	
5	Left				0.000	2.000				0.000	2.000	

NOTES: Deflection multiplier, Lambda, depends on moment sign at sustained load level and Rho' in given zone. Rho' is assumed zero because Compression Reinforcement option is NOT selected in Solve Options.

Extreme Long-term Column Strip Deflections and Corresponding Locations

	5		I I			5
	D (in), : irection '	. ,	CS	cs+lu	cs+l	Total
1	Down	Def				
-	2000	Loc				
	qU	Def	-0.025	-0.033	-0.033	-0.045
	-1	Loc	0.000	0.000	0.000	0.000
2	Down	Def	0.414	0.601	0.601	0.808
		Loc	14.000	14.000	14.000	14.000
	Up	Def				
		Loc				
3	Down	Def	0.178	0.274	0.274	0.363
		Loc	15.000	15.000	15.000	15.000
	Up	Def	-0.003	-0.004	-0.004	-0.006
		Loc	1.078	1.078	1.078	1.078
4	Down	Def	0.414	0.601	0.601	0.808
		Loc	16.000	16.000	16.000	16.000
	Up	Def				
_		Loc				
5	Down	Def				
		Loc				
	Up	Def	-0.025	-0.033	-0.033	-0.045
		Loc	0.833	0.833	0.833	0.833

NOTES: Incremental deflections due to creep and shrinkage (cs) based on sustained load level values. Incremental deflections after partitions are installed can be estimated by deflections due to: - creep and shrinkage plus unsustained live load (cs+lu), if live load applied before partitions, - creep and shrinkage plus live load (cs+l), if live load applied after partitions. Total deflections consist of dead, live, and creep and shrinkage deflections.

Extreme Long-term Middle Strip Deflections and Corresponding Locations

	D (in),	. ,				
Span D:	irection '	Value	CS	cs+lu	cs+l	Total
1	Down	Def				
		Loc				
	Up	Def	-0.025	-0.033	-0.033	-0.045
		Loc	0.000	0.000	0.000	0.000
2	Down	Def	0.241	0.339	0.339	0.459
		Loc	13.000	13.000	13.000	13.000
	Up	Def				

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		Loc				
3	Down	Def	0.060	0.101	0.101	0.131
		Loc	15.000	15.000	15.000	15.000
	Up	Def	-0.006	-0.007	-0.007	-0.010
	_	Loc	1.814	1.814	1.814	1.814
4	Down	Def	0.241	0.339	0.339	0.459
		Loc	17.000	17.000	17.000	17.000
	Up	Def				
	_	Loc				
5	Down	Def				
		Loc				
	Up	Def	-0.025	-0.033	-0.033	-0.045
	_	Loc	0.833	0.833	0.833	0.833

NOTES: Incremental deflections due to creep and shrinkage (cs) based on sustained load level values. Incremental deflections after partitions are installed can be estimated by deflections due to: - creep and shrinkage plus unsustained live load (cs+lu), if live load applied before partitions, - creep and shrinkage plus live load (cs+l), if live load applied after partitions. Total deflections consist of dead, live, and creep and shrinkage deflections.





7. Summary and Comparison of Design Results

		Hand (EFM)	spSlab
	Exterior Sp	an	
	Exterior Negative*	246.5	244.8
Column Strip	Positive	209.8	219.7
	Interior Negative*	521.9	517.6
	Exterior Negative*	0.0	0.0
Middle Strip	Positive	139.8	146.5
	Interior Negative*	174.0	172.5
	Interior Sp	an	
Calana Stain	Interior Negative*	467.6	463.6
Column Strip	Positive	118.4	120.1
Middle Strip	Interior Negative*	155.9	154.5
Middle Strip	Positive	78.9	80.1

		Table 10 - C	omparison of I	Reinforcement	Results						
Span 1	Location		ent Provided Texure	Provided fo	Reinforcement or Unbalanced t Transfer*	Total Reinforcement Provided					
		Hand	spSlab	Hand spSlab		Hand	spSlab				
	Exterior Span										
	Exterior Negative	10-#6	10-#6	5-#6	5-#6	15-#6	15-#6				
Column Strip	Positive	13-#6	13-#6	n/a	n/a	13-#6	13-#6				
Sulp	Interior Negative	22-#6	21-#6			22-#6	21-#6				
	Exterior Negative	10-#6	10-#6	n/a	n/a	10-#6	10-#6				
Middle Strip	Positive	10-#6	10-#6	n/a	n/a	10-#6	10-#6				
Surp	Interior Negative	11-#6	11-#6	n/a	n/a	11-#6	11-#6				
			Interior S	Span							
Column Strip	Positive	10-#6	10-#6	n/a	n/a	10-#6	10-#6				
Middle Strip	Positive	10-#6	10-#6	n/a	n/a	10-#6	10-#6				

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	Table 11 - Comparison of One-Way (Beam Action) Shear Check Results										
Span	V_u @	d, kips	Vu @ drop	o panel, kips	$\varphi V_c @ c$	l , kips	φV_c @ drop panel, kips				
	Hand	spSlab	Hand	spSlab	Hand	spSlab	Hand	spSlab			
Exterior	123.7	126.7	96.9	96.7	392.91	392.97	339.10	338.88			
Interior 107.8 110.9 81.0 81.0 392.91 392.97 339.10 338.88											
	$* x_u$ calculated from the centerline of the left column for each span										

Tab	le 12 - Co	mparison	of Two-W	Vay (Puncl	ning) Shea	ar Check F	Results (ai	round Colu	umns Fac	es)	
S	<i>b</i> ₁ ,	<i>b</i> ₁ , in.		, in.	b ₀	, in.	V _u ,	kips	kips c _{AB}		
Support	Hand	spSlab	Hand	spSlab	Hand	spSlab	Hand	spSlab	Hand	spSlab	
Exterior	26.56	26.56	33.13	33.13	86.26	86.25	103.6	114.6	8.18	8.18	
Interior	33.13	33.13	33.13	33.13	132.52	132.50	256.4	263.0	16.57	16.56	
Corner	26.56	26.56	26.56	26.56	53.13	53.12	60.3	60.6	6.64	6.64	
6	<i>J</i> _c ,	in. ⁴		γ_{v}	Munb,	ft-kips	Vu,	psi	φν	c, psi	
Support	Hand	spSlab	Hand	spSlab	Hand	spSlab	Hand	spSlab	Hand	spSlab	
Exterior	98,315	98,239	0.374	0.374	259	249.5	188.3	194.4	212.1	212.1	
Interior	330,800	330,520	0.400	0.400	85.70	85.07	167.9	171.7	212.1	212.1	
Corner	56,292	56,249	0.400	0.400	139.26	137.40	165.3	164.8	212.1	212.1	

Cumport	<i>b</i> ₁ , in.		b ₂	, in.	bo	, in.	V_u ,	kips	C _{A1}	в, in.
Support	Hand	spSlab	Hand	spSlab	Hand	spSlab	Hand	spSlab	Hand	spSlab
Exterior	74.44	74.44	128.88	128.88	277.76	277.75	83.92	98.24	19.95	19.95
Interior	128.88	128.88	128.88	128.88	515.52	515.50	220.37	233.91	64.44	64.44
Corner	74.44	74.44	74.44	74.44	148.88	148.87	49.36	51.53	18.61	18.61
C	<i>J</i> _c ,	in. ⁴	Vu,	psi	φν	c, psi				
Support	Hand	spSlab	Hand	spSlab	Hand	spSlab				
Exterior	1.468.983	1.468.000	35.2	39.9	156.9	156.9	1			

142.6

169.3

142.6

169.3

51.1

39.0

50.2

37.4

12,679,000

766,930

12,688,007

767,460

Interior

Corner



	Table 14 - Comparison of Immediate Deflection Results (in.)											
	Column Strip											
Snon		D	D+LL _{sus}		D +]	LL _{full}	I	L				
Span	Hand	spSlab	Hand	spSlab	Hand	spSlab	Hand	spSlab				
Exterior	0.219	0.207	0.219	0.207	0.432	0.395	0.213	0.188				
Interior	0.093	0.089	0.093	0.089	0.192	0.185	0.098	0.096				
			Ν	Aiddle Strip								
Snon		D	D +]	LLsus	D +]	LL _{full}	I	L				
Span	Hand	spSlab	Hand	spSlab	Hand	spSlab	Hand	spSlab				
Exterior	0.125	0.120	0.125	0.120	0.253	0.218	0.128	0.098				
Interior	0.031	0.030	0.031	0.030	0.064	0.071	0.033	0.040				

	Table 15	- Comparison	of Time-Depen	dent Deflection	Results	
			Column Strip			
Span	λΔ		$\Delta_{\rm cs}$, in.		$\Delta_{ ext{total}}$, in.	
	Hand	spSlab	Hand	spSlab	Hand	spSlab
Exterior	2.0	2.0	0.439	0.414	0.871	0.808
Interior	2.0	2.0	0.187	0.178	0.378	0.363
			Middle Strip	•	•	
Span	λΔ		$\Delta_{\rm cs}$, in.		Δ_{total} , in.	
	Hand	spSlab	Hand	spSlab	Hand	spSlab
Exterior	2.0	2.0	0.250	0.241	0.503	0.459
Interior	2.0	2.0	0.062	0.060	0.127	0.131

In all of the hand calculations illustrated above, the results are in close or exact agreement with the automated analysis and design results obtained from the spSlab model. Excerpts of spSlab graphical and text output are given below for illustration.

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8. Conclusions & Observations

A slab system can be analyzed and designed by any procedure satisfying equilibrium and geometric compatibility. Three established methods are widely used. The requirements for two of them are described in detail in ACI 318-14 Chapter 8 (8.2.1).

Direct Design Method (DDM) is an approximate method and is applicable to two-way slab concrete floor systems that meet the stringent requirements of <u>ACI 318-14 (8.10.2)</u>. In many projects, however, these requirements limit the usability of the Direct Design Method significantly.

The Equivalent Frame Method (EFM) does not have the limitations of Direct Design Method. It requires more accurate analysis methods that, depending on the size and geometry can prove to be long, tedious, and time-consuming.

StucturePoint's <u>spSlab</u> software program solution utilizes the Equivalent Frame Method to automate the process providing considerable time-savings in the analysis and design of two-way slab systems as compared to hand solutions using DDM or EFM.

Finite Element Method (FEM) is another method for analyzing reinforced concrete slabs, particularly useful for irregular slab systems with variable thicknesses, openings, and other features not permissible in DDM or EFM. Many reputable commercial FEM analysis software packages are available on the market today such as <u>spMats</u>. Using FEM requires critical understanding of the relationship between the actual behavior of the structure and the numerical simulation since this method is an approximate numerical method. The method is based on several assumptions and the operator has a great deal of decisions to make while setting up the model and applying loads and boundary conditions. The results obtained from FEM models should be verified to confirm their suitability for design and detailing of concrete structures.

The following table shows a general comparison between the DDM, EFM and FEM. This table covers general limitations, drawbacks, advantages, and cost-time efficiency of each method where it helps the engineer in deciding which method to use based on the project complexity, schedule, and budget.







	DDM (Hand)	EFM (Hand//spSlab)	FEM (spMats)
n sive span lengths measured center-to- of supports in each direction shall not y more than one-third the longer span shall be rectangular, with ratio of o shorter panel dimensions, measured o-center supports, not exceed 2. a offset shall not exceed 10% of the direction of offset from either axis a centerlines of successive columns Is shall be due to gravity only Is shall be uniformly distributed over			(spMats)
n sive span lengths measured center-to- of supports in each direction shall not y more than one-third the longer span shall be rectangular, with ratio of o shorter panel dimensions, measured o-center supports, not exceed 2. a offset shall not exceed 10% of the direction of offset from either axis a centerlines of successive columns Is shall be due to gravity only Is shall be uniformly distributed over		Ø	
f supports in each direction shall not y more than one-third the longer span shall be rectangular, with ratio of o shorter panel dimensions, measured o-center supports, not exceed 2. a offset shall not exceed 10% of the direction of offset from either axis a centerlines of successive columns ls shall be due to gravity only ls shall be uniformly distributed over		Ø	
o shorter panel dimensions, measured o-center supports, not exceed 2. a offset shall not exceed 10% of the direction of offset from either axis a centerlines of successive columns is shall be due to gravity only ds shall be uniformly distributed over		Ø	
direction of offset from either axis in centerlines of successive columns Is shall be due to gravity only Is shall be uniformly distributed over			
ls shall be uniformly distributed over		1	
2.5 All loads shall be uniformly distributed over an entire panel (q_u)			
ored live load shall not exceed two he unfactored dead load	Ø		
anel with beams between supports on s, slab-to-beam stiffness ratio shall be d for beams in the two perpendicular ns.	Ø		
ral integrity steel detailing	Ø	${\bf \!$	\checkmark
gs in slab systems	V	V	V
trated loads	Not permitted	V	Ø
ad arrangement (Load Patterning)	Not required	Required	Engineering judgment required based on modeling technique
cement for unbalanced slab moment to column (M _{sc})	Moments @ support face	Moments @ support centerline	Engineering judgment required based on modeling technique
ic, partial bands, mixed systems, arrangement, etc.)	Not permitted	Engineering judgment required	Engineering judgment required
Complexity		Average	Complex to very complex
Design time/costs		Limited	Unpredictable/Costly
Design Economy		Somewhat conservative	Unknown - highly dependent on modeling assumptions: 1. Linear vs. non-linear 2. Isotropic vs non-isotropic 3. Plate element choice 4. Mesh size and aspect ratio 5. Design & detailing features
General (Drawbacks)		Limited geometry	Limited guidance non-standard application (user dependent). Required significant engineering judgment
	Very limited analysis is required	Detailed analysis is required or via software (e.g. spSlab)	Unlimited applicability to handle complex situations permissible by the features of the software used (e.g. spMats)
	ment transforred to the column M (ment transferred to the column M_{sc} (M_{unb}) is the difference i	applications Detailed analysis is required or via software